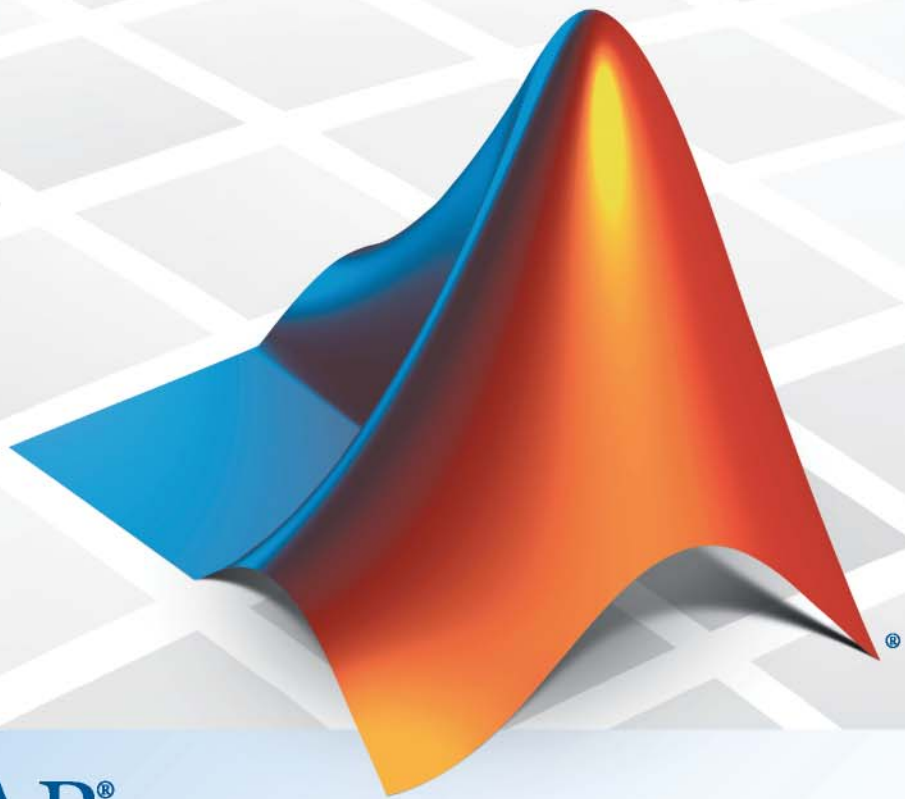


# SimBiology<sup>®</sup> 3

## Model Reference



MATLAB<sup>®</sup>

## How to Contact MathWorks



[www.mathworks.com](http://www.mathworks.com) Web  
[comp.soft-sys.matlab](mailto:comp.soft-sys.matlab) Newsgroup  
[www.mathworks.com/contact\\_TS.html](http://www.mathworks.com/contact_TS.html) Technical Support



[suggest@mathworks.com](mailto:suggest@mathworks.com) Product enhancement suggestions  
[bugs@mathworks.com](mailto:bugs@mathworks.com) Bug reports  
[doc@mathworks.com](mailto:doc@mathworks.com) Documentation error reports  
[service@mathworks.com](mailto:service@mathworks.com) Order status, license renewals, passcodes  
[info@mathworks.com](mailto:info@mathworks.com) Sales, pricing, and general information



508-647-7000 (Phone)



508-647-7001 (Fax)



The MathWorks, Inc.  
3 Apple Hill Drive  
Natick, MA 01760-2098

For contact information about worldwide offices, see the MathWorks Web site.

*SimBiology*<sup>®</sup> *Model Reference*

© COPYRIGHT 2005–2010 by The MathWorks, Inc.

The software described in this document is furnished under a license agreement. The software may be used or copied only under the terms of the license agreement. No part of this manual may be photocopied or reproduced in any form without prior written consent from The MathWorks, Inc.

FEDERAL ACQUISITION: This provision applies to all acquisitions of the Program and Documentation by, for, or through the federal government of the United States. By accepting delivery of the Program or Documentation, the government hereby agrees that this software or documentation qualifies as commercial computer software or commercial computer software documentation as such terms are used or defined in FAR 12.212, DFARS Part 227.72, and DFARS 252.227-7014. Accordingly, the terms and conditions of this Agreement and only those rights specified in this Agreement, shall pertain to and govern the use, modification, reproduction, release, performance, display, and disclosure of the Program and Documentation by the federal government (or other entity acquiring for or through the federal government) and shall supersede any conflicting contractual terms or conditions. If this License fails to meet the government's needs or is inconsistent in any respect with federal procurement law, the government agrees to return the Program and Documentation, unused, to The MathWorks, Inc.

### Trademarks

MATLAB and Simulink are registered trademarks of The MathWorks, Inc. See [www.mathworks.com/trademarks](http://www.mathworks.com/trademarks) for a list of additional trademarks. Other product or brand names may be trademarks or registered trademarks of their respective holders.

### Patents

MathWorks products are protected by one or more U.S. patents. Please see [www.mathworks.com/patents](http://www.mathworks.com/patents) for more information.

### **Revision History**

September 2005	Online only	New for Version 1.0 (Release 14SP3+)
March 2006	Online only	Updated for Version 1.0.1 (Release 2006a)
May 2006	Online only	Updated for Version 2.0 (Release 2006a+)
September 2006	Online only	Updated for Version 2.0.1 (Release 2006b)
March 2007	Online only	Rereleased for Version 2.1.1 (Release 2007a)
September 2007	Online only	Rereleased for Version 2.1.2 (Release 2007b)
October 2007	Online only	Updated for Version 2.2 (Release 2007b+)
March 2008	Online only	Updated for Version 2.3 (Release 2008a)
October 2008	Online only	Updated for Version 2.4 (Release 2008b)
March 2009	Online only	Updated for Version 3.0 (Release 2009a)
September 2009	Online only	Updated for Version 3.1 (Release 2009b)
March 2010	Online only	Updated for Version 3.2 (Release 2010a)
September 2010	Online only	Updated for Version 3.3 (Release 2010b)



## Minimal Cascade Model for a Mitotic Oscillator

# 1

<b>Goldbeter Model</b> .....	1-2
About the Goldbeter Model .....	1-2
Reaction Descriptions and Model Assumptions .....	1-3
Mathematical Model .....	1-4
<b>SimBiology Model with Rate Rules</b> .....	1-6
SimBiology Model with Rules .....	1-6
SimBiology Simulation with Rules .....	1-9
<b>SimBiology Model with Reactions</b> .....	1-10
Converting Differential Rate Equations to Reactions .....	1-10
Calculating Initial Values for Reactions .....	1-12
SimBiology Simulation with Reactions .....	1-20
<b>References</b> .....	1-21

## Model of the Yeast Heterotrimeric G Protein Cycle

# 2

<b>Objectives</b> .....	2-2
<b>Background on G Protein Cycles</b> .....	2-3
G Proteins .....	2-3
G Proteins and Pheromone Response .....	2-4
<b>Modeling a G Protein Cycle</b> .....	2-5
Reactions Overview .....	2-5
Assumptions, Experimental Data, and Units in the G Protein Model .....	2-7

<b>Building the G Protein Cycle Model</b> .....	<b>2-10</b>
Tutorial Goals .....	2-10
Opening the SimBiology Desktop .....	2-11
Saving Your Work as a SimBiology Project File .....	2-12
Adding a Reaction to the SimBiology Model .....	2-13
Determining the Reaction Rate Equation .....	2-15
Setting the Compartment Name .....	2-17
Setting Initial Amounts of Species .....	2-18
<b>Completing the SimBiology Model</b> .....	<b>2-19</b>
Reactions .....	2-19
Alternative Ways to Build Reactions in the Desktop .....	2-20
Parameters .....	2-22
Species .....	2-23
Creating a Rule for the G Protein Model .....	2-25
Verifying the Model .....	2-26
<b>Simulating the G Protein Cycle Model</b> .....	<b>2-27</b>
Setting Conditions Before Simulating the G Protein Model .....	2-27
Simulation Results for the Wild-Type Strain Model .....	2-31
<b>Creating the Mutant Strain Using a Variant</b> .....	<b>2-34</b>
Modeling the Mutant Strain .....	2-34
Applying Alternate Values Using Variants .....	2-34
Simulation Results for the Model of the Mutant Strain ...	2-35
<b>Creating a Custom Plot-Type to View Simulation</b>	
<b>Results</b> .....	<b>2-37</b>
Creating a Custom Plot .....	2-37
Visualizing Results for the Mutant Strain Using a Custom Plot .....	2-42
<b>Plotting Species from Two Different Data Sets</b> .....	<b>2-44</b>
Procedures Described in This Section .....	2-44
Plotting the Active G Protein Fraction from the Wild-Type Strain Model .....	2-44
Creating a Custom Plot to Compare the Data .....	2-45
Plotting the Active G Protein Fraction from the Model of the Mutant Strain .....	2-46

<b>Plotting Experimental Data with Simulation Data</b> . . . .	<b>2-48</b>
About the Experimental Data . . . . .	2-48
Creating a Custom Plot for Experimental Data . . . . .	2-48
Plotting the Data . . . . .	2-49
<b>References</b> . . . . .	<b>2-52</b>

## **M-Phase Control in *Xenopus* Oocyte Extracts**

# 3

<b>M-Phase Control Model</b> . . . . .	<b>3-2</b>
Synthesis Reactions . . . . .	3-2
Regulation Reactions with Active MPF . . . . .	3-2
<b>M-Phase Control Equations</b> . . . . .	<b>3-4</b>
About the Rate Equations in This Example . . . . .	3-4
Converting Differential Equations to Reactions . . . . .	3-4
Equation 1, Cyclin B . . . . .	3-6
Equation 2, M-Phase Promoting Factor . . . . .	3-6
Equation 3, Inhibited M-Phase Promoting Factor . . . . .	3-7
Equation 4, Inhibited and Activated M-Phase Promoting Factor . . . . .	3-8
Equation 5, Activated M-Phase Promoting Factor . . . . .	3-8
Equation 11, Cell Division Control 25 . . . . .	3-9
Equation 12, Wee1 Activation/Deactivation . . . . .	3-10
Equation 13, Intermediate Enzyme Activation/Deactivation . . . . .	3-10
Equation 14, APC Activation/Deactivation . . . . .	3-11
Equation 17, Rate Parameter K2 . . . . .	3-11
Equation 18, Rate Parameter Kcdc25 . . . . .	3-12
Equation 19, Rate Parameter Kwee1 . . . . .	3-12
<b>SimBiology Model with Rate and Algebraic Rules</b> . . . .	<b>3-13</b>
Overview . . . . .	3-13
Writing Differential Rate Equations as Rate Rules . . . . .	3-14
Species . . . . .	3-14
Parameters . . . . .	3-15
Rate Rule 1, Cyclin B (CycB) . . . . .	3-16
Rate Rule 2, M-Phase Promoting Factor (MPF) . . . . .	3-17

Rate Rule 3, Inhibited M-Phase Promoting Factor (pMPF) .....	3-17
Rate Rule 4, Activated but Inhibited M-Phase Promoting Factor (pMPFp) .....	3-18
Rate Rule 5, Activated M-Phase Promoting Factor (MPFp) .....	3-18
Rate Rule 11, Activated Cdc25 (Cdc25p) .....	3-18
Rate Rule 12, Inhibited Wee1 (Wee1p) .....	3-18
Rate Rule 13, Activated Intermediate Enzyme (IEp) .....	3-18
Rate Rule 14, Activated APC (APCa) .....	3-18
Algebraic Rule 17, Rate Parameter K2 .....	3-19
Algebraic Rule 18, Rate Parameter Kcdc25 .....	3-19
Algebraic Rule 19, Rate Parameter Kwee1 .....	3-19
Simulation of the M-Phase Control Model with Rules .....	3-19

### **SimBiology Model with Reactions and Algebraic**

<b>Rules</b> .....	3-21
Overview .....	3-22
Reaction 1, Synthesis of Cyclin B .....	3-22
Reaction 2, Degradation of Cyclin B .....	3-23
Reaction 3, Dimerization of Cyclin B with Cdc2 Kinase ...	3-24
Reaction 4, Degradation of Cyclin B on MPF .....	3-25
Reaction 5, Deactivation of Active MPF .....	3-26
Reaction 6, Activation of MPF .....	3-27
Reaction 7, Remove Inhibiting Phosphate from Inhibited MPF .....	3-28
Reaction 8, Inhibition of MPF by Phosphorylation .....	3-29
Reaction 11, Degradation of Cyclin B on Inhibited MPF ..	3-31
Reaction 12, Deactivation of MPF to Inhibited MPF .....	3-31
Reaction 13, Activation of Inhibited MPF .....	3-31
Reaction 15, Degradation of Cyclin B on Active but Inhibited MPF .....	3-32
Reaction 16, Inhibit MPF by Phosphorylation .....	3-32
Reaction 17, Remove Inhibiting Phosphate from Activated MPF .....	3-33
Reaction 19, Degradation of Cyclin B on Activated MPF ..	3-33
Reaction 36, Activation of Cdc25 by Activated MPF .....	3-33
Reaction 37, Deactivation of Cdc25 .....	3-34
Reaction 38, Deactivation of Wee1 by Active MPF .....	3-34
Reaction 39, Activation of Wee1 .....	3-34
Reaction 40, Activation of Intermediate Enzyme by Active MPF .....	3-35
Reaction 41, Deactivation of IE .....	3-35
Reaction 42, APC Activation by IEp .....	3-35



Reaction 43, APC Deactivation .....	<b>3-35</b>
Block Diagram of the M-Phase Control Model with Reactions .....	<b>3-36</b>
Simulation of the M-Phase Control Model with Reactions .....	<b>3-38</b>
<b>References</b> .....	<b>3-39</b>

## **Index**





# Minimal Cascade Model for a Mitotic Oscillator

---

Albert Goldbeter modified a model with enzyme cascades [Goldbeter and Koshland 1981] to fit cell cycle data from studies with embryonic cells [Goldbeter 1991]. He used this model to demonstrate thresholds with enzyme cascades and periodic behavior caused by negative feedback.

There are two SimBiology® model variations using Goldbeter's model. The first model uses the differential rate equations directly from Goldbeter's paper. The second model is built with reactions using Henri-Michaelis-Menten kinetics.

- “Goldbeter Model” on page 1-2
- “SimBiology Model with Rate Rules” on page 1-6
- “SimBiology Model with Reactions” on page 1-10
- “References” on page 1-21

## Goldbeter Model

In this section...
“About the Goldbeter Model” on page 1-2
“Reaction Descriptions and Model Assumptions” on page 1-3
“Mathematical Model” on page 1-4

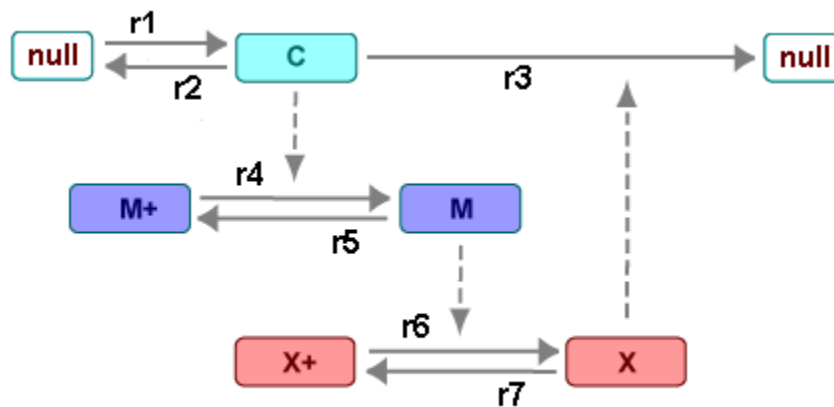
### About the Goldbeter Model

Albert Goldbeter created a simple cell division model from studies with embryonic cells [Goldbeter 1991]. This model demonstrates thresholds with enzyme cascades and periodic behavior caused by negative feedback.

There are six species in Goldbeter’s minimal mitotic oscillator model [Goldbeter 1991].

- C — Cyclin. The periodic behavior of cyclin activates and deactivates an enzyme cascade.
- M+, M — Inactive (phosphorylated) and active forms of cdc2 kinase. Kinases catalyze the addition of phosphate groups onto amino acid residues.
- X+, X — Inactive and active (phosphorylated) forms of a cyclin protease. Proteases degrade proteins by breaking peptide bonds.

The reactions are labeled r1 to r7 on the following diagram.



This model shows:

- How thresholds with cdc2 kinase activation ( $M^+ \rightarrow M$ ) and protease activation ( $X^+ \rightarrow X$ ) can occur as the result of covalent modification (for example, phosphorylation or dephosphorylation), but without the need for positive feedback.
- How periodic behavior with cdc2 kinase activation can occur with negative feedback and the time delay associated with activation/deactivation enzyme cascades.

## Reaction Descriptions and Model Assumptions

The following list describes each of the reactions in Goldbeter's minimal mitotic oscillator with some of the simplifying assumptions. For a more detailed explanation of the model, see [Goldbeter 1991].

- Cyclin (C) is synthesized at a constant rate ( $r_1$ ) and degraded at a constant rate ( $r_2$ ).
- Cyclin (C) does not complex with cdc2 kinase (M).
- Cyclin (C) activates cdc2 kinase ( $M^+ \rightarrow M$ ) by increasing the velocity of the phosphatase that activates the kinase. Inactive cdc2 kinase ( $M^+$ ) is activated by removing inhibiting phosphate groups ( $r_4$ ).

- The amount of deactivating kinase (not modeled) for the cdc2 kinase (M) is constant. Active cdc2 kinase (M) is deactivated by adding inhibiting phosphate group (r5).
- The activation of cyclin protease (X+ → X) by the active cdc2 kinase (M) is direct without other intervening cascades. Cyclin protease (X) is activated by adding phosphate groups (r6).
- The amount of deactivating phosphatase (not modeled) for the cyclin protease (X) is constant. Active cyclin protease (X) is deactivated by removing the activating phosphate groups (r7).
- The three species of interest are cyclin (C), active dephosphorylated cdc2 kinase (M), and active phosphorylated protease (X). The total amounts of (M + M+) and (X + X+) are constant.

## Mathematical Model

Goldbeter's minimal mitotic oscillator model is defined with three differential rate equations and two algebraic equations that define changing parameters in the rate equations.

### Differential Rate Equation 1, Cyclin (C)

The following differential rate equation is from [Goldbeter 1991] for cyclin (C).

$$\frac{dC}{dt} = v_i - v_d X \frac{C}{K_d + C} - k_d C$$

### Differential Rate Equation 2, Kinase (M)

The following differential rate equation is for cdc2 kinase (M). Notice that (1 - M) is the amount of inactive (phosphorylated) cdc2 kinase (M+).

$$\frac{dM}{dt} = V_1 \frac{(1 - M)}{K_1 + (1 - M)} - V_2 \frac{M}{K_2 + M}$$

$$V_1 = \frac{VM_1[C]}{K_c + [C]}$$

**Differential Rate Equation 3, Protease (X)**

Differential rate equations for cyclin protease (X). Notice that  $(1 - X)$  is the amount of inactive (unphosphorylated) cyclin protease (X+).

$$\frac{dX}{dt} = V_3 \frac{(1 - X)}{K_3 + (1 - X)} - V_4 \frac{X}{K_4 + X}$$

$$V_3 = VM_3[M]$$

## SimBiology Model with Rate Rules

### In this section...

“SimBiology Model with Rules” on page 1-6

“SimBiology Simulation with Rules” on page 1-9

### SimBiology Model with Rules

In the literature, many biological models are defined using differential rate and algebraic equations. With SimBiology software, you can enter the equations directly as SBML rules. The example in this section uses Goldbeter’s mitotic oscillator to illustrate this point.

Writing differential rate equations in an unambiguous format that a software program can understand is a fairly simple process.

- Use an asterisk to indicate multiplication. For example,  $k[a]$  is written  $k*a$ .
- Remove square brackets that indicate concentration from around species. The units associated with the species will indicate concentration (moles/liter) or amount (moles, molecules).

SimBiology software uses square brackets around species and parameter name to allow names that are not valid MATLAB® variable names. For example, you could have a species named glucose-6-phosphate dehydrogenase but you need to add brackets around the name in reaction rate and rule equations.

- Use parentheses to clarify the order of evaluation for mathematical operations. For example, do not write a Henri-Michaelis-Menten rate as  $V_m*C/K_d + C$ , because  $V_m*C$  is divided by  $K_d$  before adding  $C$ , and then  $C$  is added to the result.

The following equation is the rate rule for “Differential Rate Equation 1, Cyclin (C)” on page 1-4:

$$dC/dt = v_i - (v_d*X*C)/(K_d + C) - k_d*C$$



The following equations are the rate and repeatedAssignment rules for “Differential Rate Equation 2, Kinase (M)” on page 1-4:

$$dM/dt = (V1*Mplus)/(K1 + Mplus) - (V2*M)/(K2 + M)$$

$$V1 = (VM1*C)/(Kc + C)$$

$$Mplus = Mt - M$$

The following equations are the rate and repeatedAssignment rules for “Differential Rate Equation 3, Protease (X)” on page 1-5:

$$dX/dt = (V3*Xplus)/(K3 + Xplus) - (V4*X)/(K4 + X)$$

$$V3 = VM3*M$$

$$Xplus = Xt - X$$

## Species

The following table is a list of species in the model with their initial amounts.

The two parameters V1 and V3 are in the species list. You could enter the parameters in the parameter table with the ConstantAmount check boxes cleared. Here, the parameters are modeled as species but without reactions.

Name	InitialAmount	ConstantAmount	BoundaryCondition
C	0.01	<input type="checkbox"/>	<input type="checkbox"/>
M	0.01	<input type="checkbox"/>	<input type="checkbox"/>
Mplus	0.99	<input type="checkbox"/>	<input type="checkbox"/>
Mt	1.0	<input type="checkbox"/>	<input type="checkbox"/>
X	0.01	<input type="checkbox"/>	<input type="checkbox"/>
Xplus	0.99	<input type="checkbox"/>	<input type="checkbox"/>
Xt	1.0	<input type="checkbox"/>	<input type="checkbox"/>
V1	0.0	<input type="checkbox"/>	<input type="checkbox"/>
V3	0.0	<input type="checkbox"/>	<input type="checkbox"/>

## Parameters

The following table is a list of parameters in the model with their initial values. The **ConstantValue** property is selected for all the parameters.

Name	Value	ConstantValue
vi	0.025	<input checked="" type="checkbox"/>
kd	0.01	<input checked="" type="checkbox"/>
vd	0.25	<input checked="" type="checkbox"/>
Kd	0.02	<input checked="" type="checkbox"/>
VM1	3.0	<input checked="" type="checkbox"/>
K1	0.0050	<input checked="" type="checkbox"/>
Kc	0.5	<input checked="" type="checkbox"/>
V2	1.5	<input checked="" type="checkbox"/>
K2	0.0050	<input checked="" type="checkbox"/>
VM3	1.0	<input checked="" type="checkbox"/>
K3	0.0050	<input checked="" type="checkbox"/>
V4	0.5	<input checked="" type="checkbox"/>
K4	0.0050	<input checked="" type="checkbox"/>

## Rules

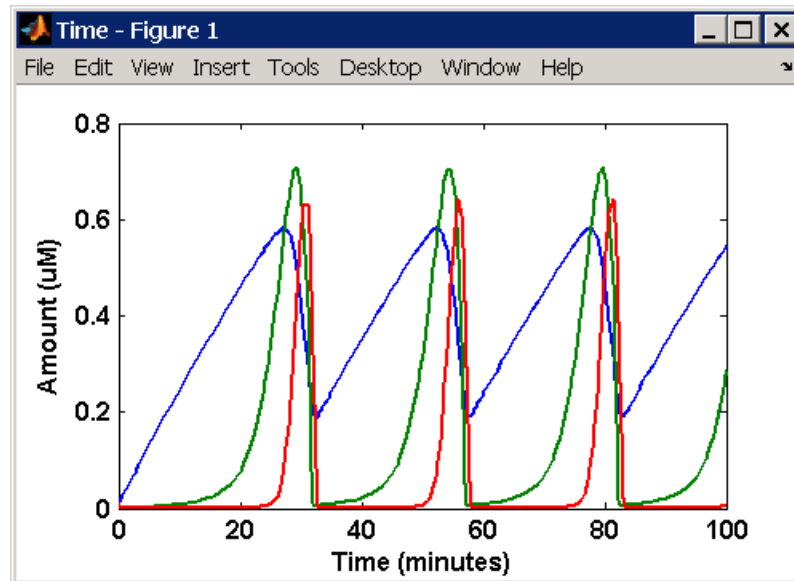
The active (M) and inactive (Mplus) forms of the kinase are assumed to be part of a conserved cycle with the total concentration (Mt) remaining constant during the simulation. You need only one differential rate equation with a mass balance equation to define the amounts of both species. Similarly, the active (X) and inactive (Xplus) forms of the protease are part of a second conserved cycle.

In the SimBiology desktop, you enter rate rules of the form  $\frac{dX}{dt} = \text{Expression}$  as  $X = \text{Expression}$ , and algebraic rules of the form " $X = \text{Expression}$ ", where X is the independent variable, as  $\text{Expression} - X$ . If you can solve for the variable, use a `repeatedAssignment` rule instead of an algebraic rule. See "What Is a repeatedAssignment Rule?" in the SimBiology documentation.

Name	Rule	RuleType
Cyclin	$C = v_i - (v_d * X * C) / (K_d + C) - k_d * C$	rate
Kinase	$M = (V_1 * M_{plus}) / (K_1 + M_{plus}) - (V_2 * M) / (K_2 + M)$	rate
	$M_{plus} = M_t - M$	repeatedAssignment
	$V_1 = (V_{M1} * C) / (K_c + C)$	repeatedAssignment
Protease	$X = (V_3 * X_{plus}) / (K_3 + X_{plus}) - (V_4 * X) / (K_4 + X)$	rate
	$X_{plus} = X_t - X$	repeatedAssignment
	$V_3 = V_{M3} * M$	repeatedAssignment

## SimBiology Simulation with Rules

This is a simulation of Goldbeter's minimal mitotic oscillator using differential rate and algebraic equations. Simulate with the sundials solver and plot species C, M, and X. For a description of the model, see "SimBiology Model with Rules" on page 1-6.



## SimBiology Model with Reactions

### In this section...

“Converting Differential Rate Equations to Reactions” on page 1-10

“Calculating Initial Values for Reactions” on page 1-12

“SimBiology Simulation with Reactions ” on page 1-20

### Converting Differential Rate Equations to Reactions

In the literature, many models are defined with differential rate equations. With SimBiology software, creating the differential equations from reactions is unnecessary; you can enter the reactions and let the software calculate the equations.

Some models are defined with differential rate equations, and you might need the reactions to be compatible with your model. Two rules you can use to convert differential rate equations to reactions are:

- **For a positive term** — The species described by the equation is placed on the right as a product, and the species in the term are placed on the left as reactants.
- **For a negative term** — The species described by the equation is placed on the left as a product, and the species in the term are also placed on the left as reactants.

You need to determine the products using additional information, for example, a reaction diagram, a description of the model, or an understanding of a reaction. If a reaction is catalyzed by a kinase, then you can conclude that the product has one or more additional phosphate groups.

A simple first-order reaction has differential rate equation  $dR/dt = +kr[P] - kf[R]$ . The negative term implies that the reaction is  $R \rightarrow ?$  with an unknown product. The positive term identifies the product and completes the reaction,  $R \leftrightarrow P$ .

### Reactions R1 to R3 from Equation E1

The differential rate equation 1 is repeated here for comparison with the reactions. See “Differential Rate Equation 1, Cyclin (C)” on page 1-4.

$$\frac{dC}{dt} = v_i - v_d X \frac{C}{K_d + C} - k_d C$$

The reaction and reaction rate equations from the differential rate equation E1 are given below:

```

r1      reaction: null -> C
        reaction rate: vi

r2      reaction: C -> null
        reaction rate: kd*C

r3      reaction: C -> null
        reaction rate: (vd*X*C)/(Kd + C)

```

### Reactions R4 and R5 from Equation E2

The differential rate equation 2 and algebraic equation 2 are repeated here for comparison with the reactions. See “Differential Rate Equation 2, Kinase (M)” on page 1-4.

$$\frac{dM}{dt} = V_1 \frac{(1-M)}{K_1 + (1-M)} - V_2 \frac{M}{K_2 + M}$$

$$V_1 = \frac{VM_1[C]}{K_c + [C]}$$

The reaction and reaction rate equations from the differential rate equation E2 are given below:

```

r4      reaction: Mplus -> M
        reaction rate: V1*Mplus/(K1 + Mplus)
        repeatedAssignment rule: V1 = VM1*C/(Kc + C)

```

r5            reaction: M -> Mplus  
               reaction rate: V2\*M/(K2 + M)

### Reactions R6 and R7 from Equation E3

The differential rate equation for equation 3 and algebraic equation 3 is repeated here for comparison with the reactions.

$$\frac{dX}{dt} = V_3 \frac{(1-X)}{K_3 + (1-X)} - V_4 \frac{X}{K_4 + X}$$

$$V_3 = VM_3 * [M]$$

The reaction and reaction rate equations from the differential rate equation E3 are given below:

r6                            reaction: Xplus -> X  
                               reaction rate: V3\*Xplus]/(K3 + Xplus)  
                               repeatedAssignment rule: V3 = VM3\*M

r7            reaction: X -> Xplus  
               reaction rate: V4\*X/(K4 + X)

### Calculating Initial Values for Reactions

After you converted the differential rate equations to the reactions and reaction rate equations, you can start to fill in initial values for the species (reactants and products) and parameters.

The initial values for parameters and amounts for species are listed with four different units in the same dimension:

- A — Original units in the Goldbeter 1991 paper.
- B — Units of concentration with time converted to second. When converting a to b, use 1 minute = 60 second for parameters.

$$\frac{X \text{ uM}}{\text{minute}} \times \frac{1e-6 \text{ mole/liter}}{1 \text{ uM}} \times \frac{1 \text{ minute}}{60 \text{ second}} = \frac{Y \text{ mole}}{\text{liter*second}}$$

- C — Units of amount as moles. When converting concentration to moles, use a cell volume of  $1e-12$  liter and assume that volume does not change.

$$\frac{Y \text{ mole}}{\text{liter*second}} \times \frac{1e-12 \text{ liter}}{1} = \frac{Z \text{ mole}}{\text{second}}$$

- D — Units of amount as molecules. When converting amount as moles to molecules, use  $6.022e23$  molecules = 1 mole.

$$\frac{Z \text{ mole}}{\text{second}} \times \frac{6.022e23 \text{ molecule}}{1 \text{ mole}} = \frac{N \text{ molecules}}{\text{second}}$$

With dimensional analysis on and unit conversion off, select all of the units for one letter. For example, select all of the As. If dimensional analysis and unit conversion are on, you can mix and match letters and get the same answer.

### Reaction 1 Cyclin Synthesis

R1		Value	Units
reaction	null -> C	----	----
reaction rate	vi	----	A. uM/minute
		----	B. mole/(liter*second)
		----	C. mole/second
		----	D. molecule/second
parameters	vi	0.025	A. uM/minute
		$4.167e-10$	B. mole/(liter*second)
		$4.167e-22$	C. mole/second
		205	D. molecule/second
species	C	0.01	A. uM
		$1e-8$	B. mole/liter
		$1.0e-20$	C. mole
		$6.022e+3$	D. molecule

### Reaction 2 Cyclin Undifferentiated Degradation

R2		Value	Units
reaction	C -> null	----	----
reaction rate	kd*C	----	A. uM/minute
		----	B. mole/(liter*second)
		----	C. mole/second
		----	D. molecule/second
parameters	kd	0.010	A. 1/minute
		1.6667e-4	B, C, D. 1/second
species	C	0.01	A. uM
		1e-8	B. mole/liter
		1.0e-20	C. mole
		6.022e+3	D. molecule

### Reaction 3 Cyclin Protease Degradation

R3		Value	Units
reaction	C -> null	----	----
reaction rate	$(vd*X*C) / (Kd + C)$	----	A. uM/minute
		----	B. mole/(liter*second)
		----	C. mole/second
		----	D. molecule/second
parameter	vd	0.25	A. 1/minute
		0.0042	B, C, D. 1/second
parameter	Kd	0.02	A. uM
		2.0e-8	B. mole/liter
		2.0e-020	C. mole



<b>R3</b>		<b>Value</b>	<b>Units</b>
		12044	D. molecule
species	C (substrate)	0.01	A. uM
		1e-8	B. mole/liter
		1.0e-20	C. mole
		6.022e+3	D. molecule
species	X (enzyme)	0.01	A. uM
		1e-8	B. mole/liter
		1.0e-20	C. mole
		6.022e+3	D. molecule

### Reaction 4 Cdc2 Kinase Activation

<b>R4</b>		<b>Value</b>	<b>Units</b>
reaction	Mplus -> M	----	----
reaction rate	$(V1 * Mplus) / (K1 + Mplus)$	----	A. uM/minute
		----	B. mole/(liter*second)
		----	C. mole/second
		----	D. molecule/second
repeatedAssignment rule	$V1 = (VM1 * C) / (Kc + C)$	----	
parameter	V1 (variable by rule)	0.00	A. uM/minute
			B. mole/(liter*second)
			C. mole/second
			D. molecule/second
parameter	VM1	3.0	A. uM/minute
		5.0e-8	B. mole/(liter*second)

<b>R4</b>		<b>Value</b>	<b>Units</b>
parameter	Kc	5.0000e-020	C. mole/second
		30110	D. molecule/second
		0.5	A. uM
		5.0000e-7	B. mole/liter
		5.0e-19	C. mole
parameter	K1	3.011e+5	D. molecule
		0.005	A. uM
		5e-9	B. mole/liter
		5e-21	C. mole
		3.011e+3	D. molecule
species	Mplus (inactive substrate)	0.99	A. uM
		9.9e-7	B. mole/liter
		9.9e-19	C. mole
		5.962e+5	D. molecule
		0.01	A. uM
species	M (active product)	1e-8	B. mole/liter
		1.0e-20	C. mole
		6.022e+3	D. molecule
		0.01	A. uM
		1e-8	B. mole/liter
species	C	1.0e-20	C. mole
		6.022e+3	D. molecule
		0.01	A. uM
		1e-8	B. mole/liter
		1.0e-20	C. mole
		6.022e+3	D. molecule

**Reaction 5 Cdc2 Kinase Deactivation**

<b>R5</b>		<b>Value</b>	<b>Units</b>
reaction	M -> M_plus	----	----
reaction rate	$(V2 * M) / (K2 + M)$	----	A. uM/minute
		----	B. (mole/liter-second)
		----	C. mole/second
		----	D. molecule/second
parameter	V2	1.5	A. uM/minute
		2.5000e-008	B. mole/liter-second
		2.5000e-020	C. mole/second
		15055	D. molecule/second
parameter	K2	0.005	A. uM
		5.0000e-009	B. mole/liter
		5.0000e-021	C. mole
		3011	D. molecule
		1.0e-20	C. mole
species	Mplus (inactive)	0.99	A. uM
		9.9e-7	B. mole/liter
		9.9e-19	C. mole
		5.962e+5	D. molecule
species	M (active)	0.01	A. uM
		1e-8	B. mole/liter
		1.0e-20	C. mole
		6.022e+3	D. molecule

### Reaction 6 Protease Activation

R6		Value	Units
reaction	Xplus -> X	----	----
reaction rate	$(V3 \cdot Xplus) / (K3 + Xplus)$	----	A. uM/minute B. mole/(liter*second) C. mole/second D. molecule/second
repeatedAssignment rule	$V3 = VM3 \cdot M$	----	
parameter	V3 (variable by rule)		A. uM/minute B. mole/liter-second C. mole/second D. molecule/second
parameter	VM3	1.0 0.0167	A. 1/minute B, C, D. 1/second
parameter	K3	0.005 5e-9 5e-21 3.011e+3	A. uM B. mole/liter C. mole D. molecule
species	Xplus (inactive substrate)	0.99 9.9e-7 9.9e-19 5.962e+5	A. uM B. mole/liter C. mole D. molecule
species	X (active product)	0.01 1e-8 1.0e-20 6.022e+3	A. uM B. mole/liter C. mole D. molecule

<b>R6</b>		<b>Value</b>	<b>Units</b>
species	M (enzyme)	0.01	A. uM
		1e-8	B. mole/liter
		1.0e-20	C. mole
		6.022e+3	D. molecule

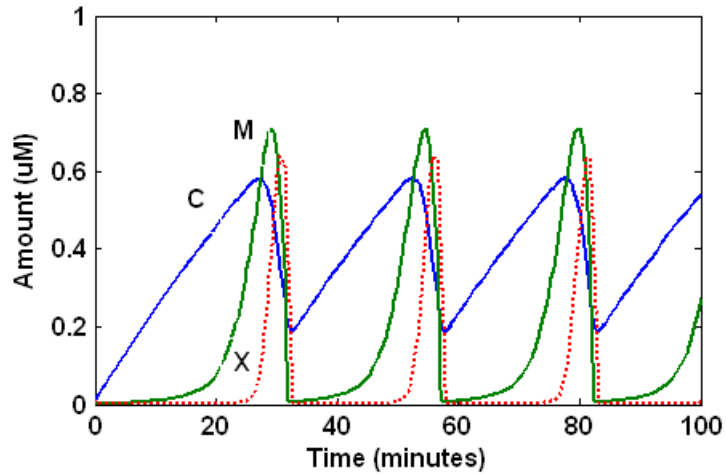
### Reaction 7 Protease Deactivation

<b>R7</b>		<b>Value</b>	<b>Units</b>
reaction	X -> X_plus	----	----
reaction rate	$(V4 * X) / (K4 + X)$	----	A. uM/minute
		----	B. mole/(liter*second)
		----	C. mole/second
		----	D. molecule/second
parameter	V4	0.5	A. uM/minute
		8.3333e-009	B. mole/(liter*second)
		8.3333e-021	C. mole/second
		5.0183e+003	D. molecule/second
parameter	K4	0.005	A. uM
		5e-9	B. mole/liter
		5e-21	C. mole
		3011	D. molecule
species	Xplus (inactive)	0.99	A. uM
		9.9e-7	B. mole/liter
		9.9e-19	C. mole
		5.962e+5	D. molecule
species	X (active)	0.01	A. uM
		1e-8	B. mole/liter

R7	Value	Units
	1.0e-20	C. mole
	6.022e+3	D. molecule

## SimBiology Simulation with Reactions

This is a simulation of Goldbeter's minimal mitotic oscillator with rate and algebraic equations. Simulate with the `sundials` solver and plot species C, M, and X. For a description of the model, see "SimBiology Model with Reactions" on page 1-10.



---

## References

- [1] Goldbeter A. (1991), "A minimal cascade model for the mitotic oscillator involving cyclin and cdc2 kinase," *Proceedings of the National Academy of Sciences USA*, 88:9107-9111.
- [2] Goldbeter A., Koshland D. (1981), "An amplified sensitivity arising from covalent modification in biological systems," *Proceedings of the National Academy of Sciences USA*, 78:6840-6844.
- [3] Goldbeter A., Koshland D. (1984), "Ultrasensitivity in biochemical systems controlled by covalent modification," *The Journal of Biological Chemistry*, 259:14441-14447.
- [4] Goldbeter A., home page on the Web,  
<http://www.ulb.ac.be/sciences/utc/GOLDBETER/agoldbet.html>
- [5] Murray A.W., Kirschner M.W. (1989), "Cyclin synthesis drives the early embryonic cell cycle," *Nature*, 339:275-280.





# Model of the Yeast Heterotrimeric G Protein Cycle

---

- “Objectives” on page 2-2
- “Background on G Protein Cycles” on page 2-3
- “Modeling a G Protein Cycle” on page 2-5
- “Building the G Protein Cycle Model” on page 2-10
- “Completing the SimBiology Model” on page 2-19
- “Simulating the G Protein Cycle Model” on page 2-27
- “Creating the Mutant Strain Using a Variant” on page 2-34
- “Creating a Custom Plot-Type to View Simulation Results” on page 2-37
- “Plotting Species from Two Different Data Sets” on page 2-44
- “Plotting Experimental Data with Simulation Data” on page 2-48
- “References” on page 2-52

### Objectives

SimBiology software lets you build a model using a conceptual framework of biochemical reactions that describe a biological process. You can plot experimental data on top of your model's simulation results to investigate the validity of your model, make predictions based on the model, and test your hypotheses.

Using concepts and data from the published work of Yi and colleagues [Yi et al. 2003], this tutorial shows you how to:

- 1 Build a model using the SimBiology graphical user interface (GUI).
- 2 Apply an alternate value during simulation to create a variation of the model (for example, wild-type versus mutant).
- 3 Simulate and save the data from the two models.
- 4 Compare the two simulations.
- 5 Compare the simulation results with the experimental data.

## Background on G Protein Cycles

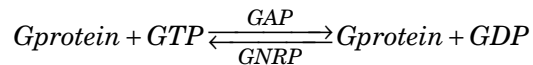
### In this section...

“G Proteins” on page 2-3

“G Proteins and Pheromone Response” on page 2-4

### G Proteins

Cells rely on signal transduction systems to communicate with each other and to regulate cellular processes. G proteins are GTP-binding proteins that are involved in the regulation of many cellular processes. There are two known classes of G proteins: the monomeric G proteins (one GTPase), and the heterotrimeric G proteins (three different monomers). The G proteins usually facilitate a step requiring energy. This energy is supplied by the hydrolysis of GTP by a GTPase activating protein (GAP). The exchange of GDP for GTP is catalyzed by a guanine nucleotide releasing protein (GNRP) [Alberts et al. 1994].



G protein-coupled receptors (GPCRs) are the targets of many pharmaceutical agents. Some estimates suggest that 40 to 50% of currently marketed drugs target GPCRs and that 40% of current drug discovery focus is on GPCR targets. Some examples include those for reducing stomach acid (ranitidine which targets histamine H2 receptor), migraine (sumatriptan, which targets a serotonin receptor subtype), schizophrenia (olanzapine, which targets serotonin and dopamine receptors), allergies (desloratadine, which targets histamine receptors). One approach in pharmaceutical research is to model signaling pathways to analyze and predict both downstream effects and effects in related pathways. This tutorial examines model building and analysis of the G protein cycle in the yeast pheromone response pathway using the SimBiology desktop.

### **G Proteins and Pheromone Response**

In the yeast *Saccharomyces cerevisiae*, G protein signaling in pheromone response is a well characterized signal transduction pathway. The pheromone secreted by *alpha* cells activates the G protein-coupled  $\alpha$ -factor receptor (Ste2p) in *a* cells which results in a variety of cell responses including cell-cycle arrest and synthesis of new proteins. The authors of the study performed a quantitative analysis of this cycle, compared the regulation of G protein activation in wild-type yeast haploid *a* cells with cells containing mutations that confer supersensitivity to  $\alpha$ -factor. They analyzed the data in the context of cell-cycle arrest and pheromone-induced transcriptional activation and developed a mathematical model of the G protein cycle that they used to estimate rates of activation and deactivation of active G protein in the cell.

## Modeling a G Protein Cycle

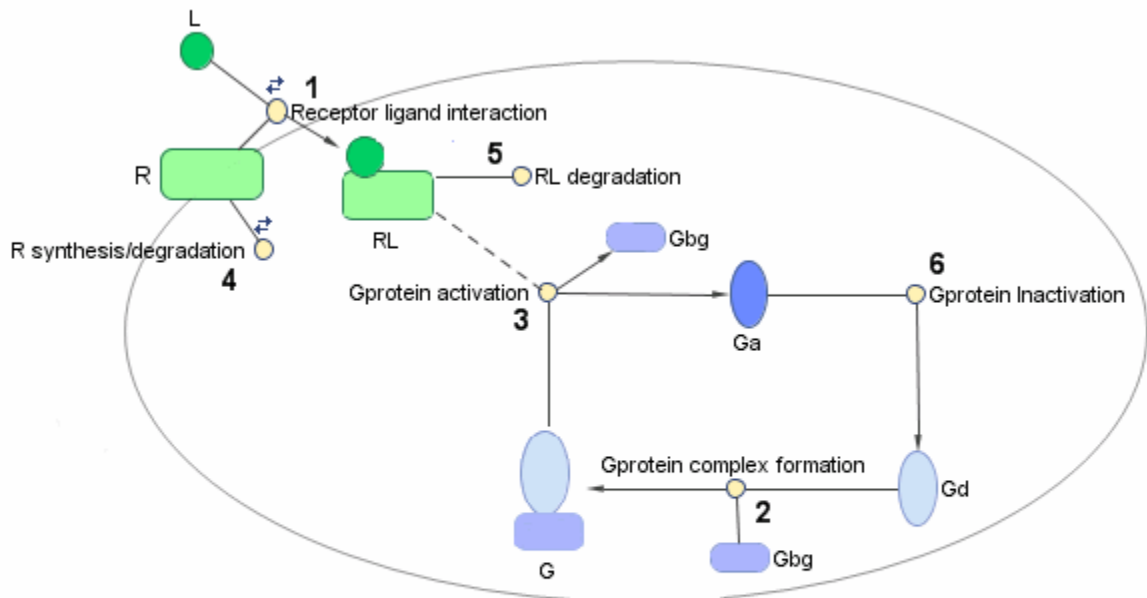
In this section...
“Reactions Overview” on page 2-5
“Assumptions, Experimental Data, and Units in the G Protein Model” on page 2-7

### Reactions Overview

Systems biologists represent biological pathways and processes as reactions with reaction rates, and treat the components of these pathways as individual species.

The G protein cycle in the yeast pheromone-response pathway can be condensed into a set of biochemical reactions. These reactions are complex formation, transformation, or disassociation reactions that Yi and colleagues [Yi et al. 2003] use to simplify and describe the system. In this example,  $\alpha$ -factor,  $\alpha$ -factor receptor, and the G protein subunits are all treated as species participating in reactions. The system can be graphically represented as follows.

## 2 Model of the Yeast Heterotrimeric G Protein Cycle



Graphical Representation of the G protein cycle in yeast pheromone response. The numbers represent reaction numbers referenced in the text. L = Ligand (alpha factor), R = alpha-factor receptor, Gbg = free levels of G-beta:G-gamma complex, Ga = active G-alpha-GTP, Gd = inactive G-alpha-GDP, G = inactive Gbg:Gd complex.

The following table shows you the reactions used to model the G protein cycle and the corresponding rate constants (rate parameters) for each reaction. For reversible reactions, the forward rate parameter is listed first.

No.	Name	Reaction	Rate Parameters
1	Receptor-ligand interaction	$L + R \leftrightarrow RL$	$k_{RL}, k_{RLm}$
2	Heterotrimeric G protein formation	$Gd + Gbg \rightarrow G$	$k_{G1}$
3	G protein activation	$RL + G \rightarrow Ga + Gbg + RL$	$k_{Ga}$

No.	Name	Reaction	Rate Parameters
4	Receptor synthesis and degradation	$R \leftrightarrow \text{null}$	kRdo, kRs
5	Receptor-ligand degradation	$RL \rightarrow \text{null}$	kRD1
6	G protein inactivation	$Ga \rightarrow Gd$	kGd

Note that in reaction 3 (G protein activation), RL appears on both sides of the reaction. This is because RL is treated as a modifier or catalyst, and the model assumes that there is no synthesis or consumption of RL in this reaction.

The authors use a set of ordinary differential equations (ODEs) to describe the system. In the software, you can represent the biological pathway as a system of biochemical reactions and the software creates the ODEs for you. Alternatively, if you have a set of ODEs that describe your system you can enter these as rate rules. For an example of modeling using rate rules, see “SimBiology Model with Rate Rules” on page 1-6.

## Assumptions, Experimental Data, and Units in the G Protein Model

The authors have obtained experimental data either through their own measurements or through published literature. As with any other model, the G protein cycle model simplifies the biological process while also trying to reconcile the experimental data. Consider these points:

- Reaction 2 — Binding and formation of the heterotrimeric G protein complex is treated as a single-step reaction.
- Reaction 3 — Activation of G protein is modeled as a single-step. Guanine nucleotide exchange factors (GEFs) are not modeled.
- Reactions 3 and 6 — The parameters for the rate of G protein activation and deactivation (kGa and kGd) have been estimated based on the dose response curves in the reference paper. The SimBiology model being built in this tutorial directly uses those values.

- Reactions 4 and 5 — Receptor synthesis and degradation are handled purely as two simple reaction steps.
- Reaction 6 — Deactivation of G protein by the regulator of G protein signaling (RGS) protein Sst2p is modeled as a single step. Sst2p is not modeled.

The reaction is modeled with an estimated reaction rate of  $0.11 \text{ s}^{-1}$  in the Sst2p containing wild-type strain. The uncatalyzed reaction rate is estimated to be  $0.004 \text{ s}^{-1}$  in a strain with a deletion of SST2 (*sst2Δ*, mutant strain).

- Free GDP, GTP, and Pi are not included in the model.

This tutorial shows you how to plot the experimental data over the simulation plot of the active G protein fraction. You can estimate the values of the experimental data of interest for this example from the coordinates of the plots found in Figure 5 of the reference paper [Yi et al. 2003]. The following values were obtained by comparing the coordinates of the standards with those of the unknowns in the figure.

Time	Fraction of Active G $\alpha$ (Experimental)
0	0.00
10	0.35
30	0.40
60	0.36
110	0.39
210	0.33
300	0.24
450	0.17
600	0.20



---

**Note** The SimBiology **Dimensional Analysis** feature is not used in this tutorial. For this tutorial, the values of all species are converted to have the unit `molecule`, and all rate parameters are converted to have either the unit `1/second` or the units `1/(molecule*second)`, depending on whether the reaction is first or second order. You should leave the **InitialAmountUnits** box for species and the **ValueUnits** box for rate parameters empty for the models in this tutorial.

---

## Building the G Protein Cycle Model

### In this section...

“Tutorial Goals” on page 2-10

“Opening the SimBiology Desktop” on page 2-11

“Saving Your Work as a SimBiology Project File” on page 2-12

“Adding a Reaction to the SimBiology Model” on page 2-13

“Determining the Reaction Rate Equation” on page 2-15

“Setting the Compartment Name” on page 2-17

“Setting Initial Amounts of Species” on page 2-18

### Tutorial Goals

This section shows you how to build the example yeast heterotrimeric G protein models using the SimBiology desktop GUI (graphical user interface). For an overview of the SimBiology desktop, [click here](#). The SimBiology desktop is also called “the desktop” in the SimBiology documentation.

This section assumes that you are starting with an untitled `Project` and a default `Untitled Model Session` in the SimBiology desktop.

If you are running the `gprotein.sbproj` file that contains the models in this tutorial, see “Simulating the G Protein Cycle Model” on page 2-27 for details about the simulation and analysis of these models.

This example uses the yeast G protein cycle [Yi et al. 2003] to illustrate model building and analysis. The goals of this tutorial are the following:

- 1** Build a model of the wild-type strain (TMY101) that has the `SST2` gene. This strain shows a catalyzed rate of deactivation of `Gα`. `Gα` is represented as `Gα` in the model.
- 2** Store alternate values in a **Variant** to create a different model for the mutant strain (`sst2Δ`, TMY111) that shows an uncatalyzed rate of G-Protein inactivation.

- 3** Simulate and save the data from the two models.
- 4** Compare the active G protein fractions in the two simulations.
- 5** Compare the simulation results for active G protein fractions with experimental data.

For additional help in each procedure, select **Help > SimBiology Desktop Help**.

## Opening the SimBiology Desktop

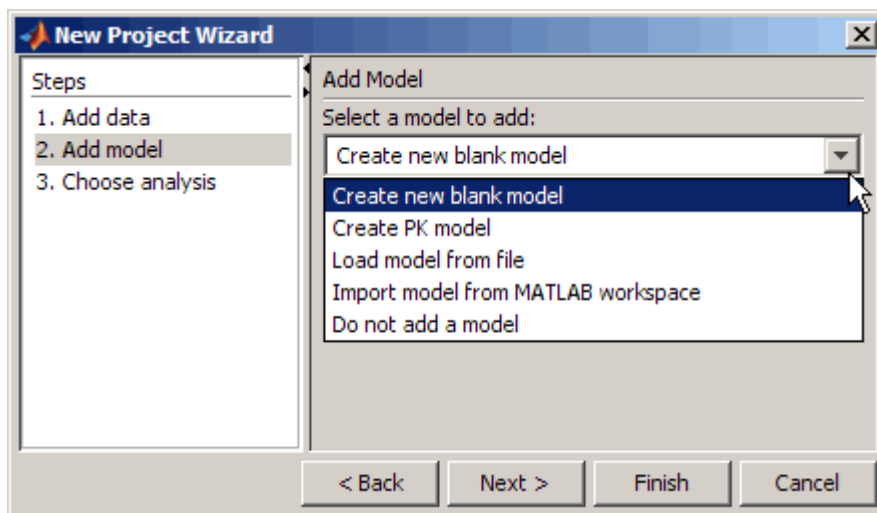
The procedures in this tutorial are performed in the SimBiology desktop. The desktop provides access to command-line functionality through a graphical user interface. You can open the desktop from the MATLAB Command Window.

- 1** In the MATLAB Command Window, type:

```
simbiology
```

The SimBiology desktop opens.

- 2** Select **File > New Project**. The New Project Wizard opens.
- 3** Skip the **Add Data** step for this example and select **Add Model**.
- 4** In the **Add Model** pane, from the **Select a model to add** list, select **Create a new blank model**. This selection creates a **Model Session** containing one compartment (at least one compartment is required for all models). You will later add model components such as species, reactions, rules, and events to the model.



**5** In the **Model Name** box, type the name for your model.

Yeast\_G\_Protein\_wt

**6** Click **Next**.

**7** In the **Choose Analysis** pane, leave the default selection (**Simulate model**) selected for the analysis tasks to add to the model and click **Finish**.

A new project with the selected specifications opens.

### **Saving Your Work as a SimBiology Project File**

Project (.sbproj) is the file format used to save one or more model sessions. Projects let you save custom settings, notes, and data associated with your models.

Save your work as a project now so that you can access this file later.

- 1** Select **File > Save Project As** to open the Save SimBiology Project dialog box.
- 2** Browse to the folder in which you want to save your projects, enter a name for the project file, and then click **Save**.

yeast\_g\_protein\_cycle.sbproj

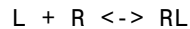
## Adding a Reaction to the SimBiology Model

The next steps show how to add a reaction and determine the reaction rate equation for your model.

This example shows the first reaction.

Name	Reaction	Rate Parameters
Receptor-ligand interaction	$L + R \leftrightarrow RL$	kRL, kRLm

- 1 In the **Project Explorer**, expand **SimBiology Model** and click **Reactions** to open the **Reactions** pane.
- 2 Enter the reaction in the **Enter Reaction** box, and click **Add**.



A red indicator appears to the right of the table. Move the pointer over the indicator for the reaction, to get more information about the reason for the indicator. In this case, the indicator shows that the reaction rate is invalid. The next section shows how to define the reaction rate.

- 3 Double-click the **Name** box, and type the name for your reaction. For example:

Receptor-Ligand Interaction

- 4 In the reaction table, from the **KineticLaw** list, select **MassAction**.

Your screen should now resemble the following figure.

Name	Reaction	KineticLaw	ReactionRate
1 Receptor-Ligand Interaction	$L + R \leftrightarrow RL$	MassAction	

**Settings** | Description

Reaction:  Reversible

$L + R \leftrightarrow RL$

KineticLaw: MassAction      Expression:  $(\text{Forward Rate Parameter}) * (\text{MassAction Species}) - (\text{Reverse Rate Parameter})$

Map between KineticLaw Parameters and Parameter Names:

Kinetic Law Parameter	Parameter Name	Value	Scope	ValueUnits
1 Forward Rate Parameter				
2 Reverse Rate Parameter				

Map between KineticLaw Species and Species Names:

Kinetic Law Species	Species Name	InitialAmount	Scope	InitialAmountUnits
1 MassAction Species	L	0.0	unnamed	
2 MassAction Species	R	0.0	unnamed	
3 MassAction Species	RL	0.0	unnamed	

ReactionRate: (ReactionRate not fully defined. Map parameters and species above to define.)

Name: Receptor-Ligand Interaction

Active (Select if the reaction is enabled during the simulation.)

Notice the following in the **Settings** tab:

- Because this reaction is reversible, the **Reversible** check box is selected by default when you enter the reaction.
- All the reactions in this example model are included in the simulation and, therefore, have the **Active** check box selected. By default, the **Active** check box is selected.

---

**Tip** You must use spaces between the species and the characters in the reaction. If you have a reaction with different stoichiometry, for example,  $2 A + B \leftrightarrow 3 AB$ , you must have a space between the stoichiometric coefficient and the species name for the reaction rate to be accurately determined. Otherwise, the coefficients are considered as part of the species name.

---

## Determining the Reaction Rate Equation

The desktop populates the reaction rate column after you specify the kinetic law and the rate parameters of the reaction.

To assign and configure the kinetic law and the rate parameters, do the following in the **Reactions** pane:

- 1** In the **Map between KineticLaw Parameters and Parameter Names** section, locate the **Forward Rate Parameter** row, double-click the **Parameter Name** cell, type **kRL** and press **Enter**.
- 2** In the **Reverse Rate Parameter** row, double-click the **Parameter Name** cell, type **kRLm** and press **Enter**.

Name	Reaction	KineticLaw	ReactionRate
1 Receptor-Ligand Interaction	$L + R \leftrightarrow RL$	MassAction	$k_{RL} * L * R - k_{RLm} * RL$

**Settings** | Description

Reaction:  Reversible

$L + R \leftrightarrow RL$

KineticLaw: MassAction      Expression:  $(ter) * (MassAction Species) - (Reverse Rate Parameter) * (MassAction Species)$

Map between KineticLaw Parameters and Parameter Names:

	Kinetic Law Parameter	Parameter Name	Value	Scope	ValueUnits
1	Forward Rate Parameter	kRL	1.0	L + R <-> RL	
2	Reverse Rate Parameter	kRLm	1.0	L + R <-> RL	

Map between KineticLaw Species and Species Names:

	Kinetic Law Species	Species Name	InitialAmount	Scope	InitialAmountUnits
1	MassAction Species	L	0.0	unnamed	
2	MassAction Species	R	0.0	unnamed	
3	MassAction Species	RL	0.0	unnamed	

ReactionRate:  $k_{RL} * L * R - k_{RLm} * RL$

Name: Receptor-Ligand Interaction

Active (Select if the reaction is enabled during the simulation.)

- The desktop updates the **ReactionRate** column to show  $k_{RL} * L * R - k_{RLm} * RL$ , and the indicator is now green showing that this reaction is completely defined.
- For this example, **Scope** of all the parameters is at the kinetic law level. The desktop displays the reaction in the **Scope** box.
- The desktop automatically selects the species when you select MassAction kinetic law. For other kinetic laws, you should enter the species to be included in the rate equation.

**3** In the **Value** cell, enter the following parameter values:

$$k_{RL} = 3.32E-18 \text{ and } k_{RLm} = 0.01$$



Enter Reaction:  Add Delete

Name	Reaction	KineticLaw	ReactionRate
1 Receptor ligand interaction	L + R <-> RL	MassAction	kRL*L*R - kRLm*RL

**Settings** | **Description**

Reaction:  Reversible

L + R <-> RL

KineticLaw:  Expression:

MassAction  [(Forward Rate Parameter)\*(MassAction Species) - (Reverse Rate Parameter)\*(M

Map between KineticLaw Parameters and Parameter Names:

	Kinetic Law Parameter	Parameter Name	Value	Scope	ValueUnits
1	Forward Rate Parameter	kRL	3.32E-18	L + R <-> RL	
2	Reverse Rate Parameter	kRLm	0.01	L + R <-> RL	

## Setting the Compartment Name

All models created in the desktop contain a compartment by default. The process of adding a reaction automatically adds the reaction species to a compartment in the model. If there are multiple compartments in the model, you must specify the reactants and products using qualified names (*compartmentName.speciesName*). For example, nucleus.DNA denotes the species DNA in the compartment nucleus.

This example contains only one compartment. To rename the compartment:

- 1 In the **Project Explorer**, click **Compartments**.
- 2 In the **Name** cell, double-click and type a name for the compartment, and then press **Enter**.

```
yeast_cell
```

The compartment table updates with the new name.

Use the default values for the **Owner**, **Capacity**, and **CapacityUnits** cells.

## Why Use Default Values

- **Owner** lets you define whether the compartment is within another compartment. This model has only one compartment within which you

define all the species. No **Owner** means that the compartment is a top-level compartment.

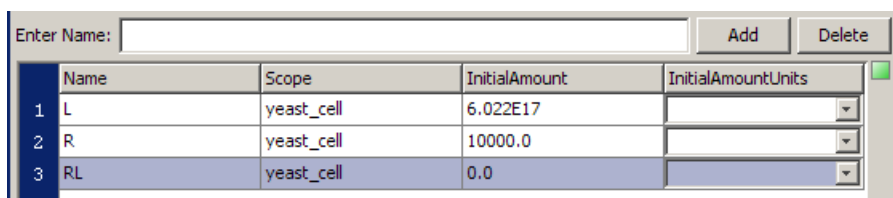
- **Capacity** lets you enter the compartment size, such as volume, length, or area. In this model, species are defined in amounts, the reaction rate dimensions are amount/time, and the model assumes that compartment volume is constant. Thus, all the values and the units are internally consistent with each other and the compartment volume can use the default value of 1.0.
- **CapacityUnits** lets you specify the units for **Capacity**, which are not needed for this example.

### Setting Initial Amounts of Species

You can set the initial amounts of all the model species in the **Species** pane.

Name	InitialAmount
L	6.022E17
R	10000.0
RL	0.0

- 1 In the **Project Explorer**, expand **Compartments** and click **yeast\_cell Species**.
- 2 In the **Species** pane, double-click in each **InitialAmount** cell and enter the preceding values.



Notice that the **Scope** column lists the name of the compartment containing the species.

You now have a complete reaction with all components added and defined.

## Completing the SimBiology Model

### In this section...

“Reactions” on page 2-19

“Alternative Ways to Build Reactions in the Desktop” on page 2-20

“Parameters” on page 2-22

“Species” on page 2-23

“Creating a Rule for the G Protein Model” on page 2-25

“Verifying the Model” on page 2-26

### Reactions

The previous sections showed you how to enter the first reaction for the yeast G protein cycle model and configure the reaction rate equation. Repeat the procedures to add the rest of the reactions, parameters, and species values as described in the previous sections, and create a rule to specify the ratio of active G protein that corresponds to the ratio determined experimentally in the referenced study [Yi et al. 2003].

Add reactions 2 to 6 listed in this table, set the kinetic law for each reaction to `MassAction`, create parameters, and configure the reaction rate using the procedure for “Determining the Reaction Rate Equation” on page 2-15.

No.	Name	Reaction	Rate Parameters
1	Receptor-ligand interaction	$L + R \leftrightarrow RL$	$k_{RL}, k_{RLm}$
2	Heterotrimeric G protein formation	$G_d + G_{bg} \rightarrow G$	$k_{G1}$
3	G protein activation	$RL + G \rightarrow Ga + G_{bg} + RL$	$k_{Ga}$
4	Receptor synthesis and degradation	$R \leftrightarrow null$	$k_{Rdo}, k_{RS}$

No.	Name	Reaction	Rate Parameters
5	Receptor-ligand degradation	RL -> null	kRD1
6	G protein inactivation	Ga -> Gd	kGd

Your reaction table should resemble the following figure.

Enter Reaction: <input type="text"/>				Add	Delete
	Name	Reaction	KineticLaw	ReactionRate	
1	Receptor-ligand	L + R <-> RL	MassAction	kRL*L*R - kRLm*RL	
2	Heterotrimeric G protein formation	Gd + Gbg -> G	MassAction	kG1*Gd*Gbg	
3	G protein_activation	RL + G -> Ga + Gbg + RL	MassAction	kGa*RL*G	
4	Receptor synthesis and degradation	R <-> null	MassAction	kRdo*R - kRs	
5	Receptor-Ligand degradation	RL -> null	MassAction	kRD1*RL	
6	G protein inactivation	Ga -> Gd	MassAction	kGd*Ga	

The next section describes other ways you can build reactions in the desktop. If you want to continue building the model, skip the next section and go to “Parameters” on page 2-22.

## Alternative Ways to Build Reactions in the Desktop

This optional section shows you some alternative methods to build a reaction in the **Reactions** pane. Use the examples above to try out these methods. If you have finished entering the reactions for the model, proceed to “Parameters” on page 2-22.

The **Reactions** pane has several dialog boxes that are convenient for building reactions.

### Building a Reaction

You can graphically build a reaction using the Reaction Builder.

- 1 If you are not already in the **Reactions** pane, in the **Project Explorer** click **Reactions**.


- 2 Click **Build** to open the Reaction Builder dialog box.
- 3 Select a species from the **Available Species** list and click the **Reactant** or **Product** button.
- 4 To edit stoichiometric relationships, click in the **Stoich** column and type.
- 5 Select the **Reversible** check box if the reaction is reversible.
- 6 Click **Add** to continue editing within the Reaction Builder. Click **OK** to finish and return to the **Reactions** pane.

### Creating a Binding Reaction

Use the **Bind** button to create a bound product from two reactant species.

- 1 If you are not already in the **Reactions** pane, in the **Project Explorer** click **Reactions**.
- 2 In the **Enter Reaction** box, enter the reactant species.

lactose + lactase

- 3 Click the  **Bind** button. The software writes the product as a compound name, with a colon between reactant names to indicate binding.

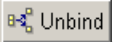
lactose:lactase

### Creating an Unbinding Reaction

Use the **Unbind** button to create two product species from a bound reactant.

- 1 If you are not already in the **Reactions** pane, in the **Project Explorer** click **Reactions**.
- 2 In the **Enter Reaction** box, enter the reactant species.

lactose:lactase

- 3 Click the  **Unbind** button. The software writes the product names with a + between them to indicate unbinding.

lactose + lactase

## Parameters

In the **Reactions** pane, after you create parameters in the **Settings** tab, you can set the value of the parameter in the parameters table.

Alternatively, you can set all the parameters in the **Parameters** pane. In the **Project Explorer**, click **Parameters** to open the **Parameters** pane.

Use the following values for rate parameters.

### Parameter Value Table

Name	Value
kRLm	0.01
kRL	3.32E-18
kRdo	4.0E-4
kRs	4.0
kRD1	0.0040
kG1	1.0
kGa	1.0E-5
kGd	0.11

To be consistent with units for kRL, RL and L, the value for kRL is converted from the published value,  $2.0E6M^{-1}s^{-1}$ , to  $3.32E-18$  with units  $1/(molecule*second)$  (assuming a volume of unity).

Enter Name: <input type="text"/>					Add	Delete
	Name	Scope $\Delta$	Value	ValueUnits		
1	kRLm	L + R $\leftrightarrow$ RL	0.01			
2	kRL	L + R $\leftrightarrow$ RL	3.32E-18			
3	kRdo	R $\leftrightarrow$ null	4.0E-4			
4	kRs	R $\leftrightarrow$ null	4.0			
5	kRD1	RL $\rightarrow$ null	0.0040			
6	kG1	Gd + Gbg $\rightarrow$ G	1.0			
7	kGa	RL + G $\rightarrow$ Ga + Gbg + RL	1.0E-5			
8	kGd	Ga $\rightarrow$ Gd	0.11			

## Species

Set the species amounts in the **Species** pane. In the **Project Explorer**, click **yeast\_cell Species** to access this pane.

- Note that the process of adding reactions resulted in species automatically being added to the species list, with default amounts set to 0.0. Double-click each **InitialAmount** cell to change the values to those given in the table.
- The amount of L ( $\alpha$ -factor) used in the experiments is 1 M. This value when converted to **molecule** (assuming a volume of unity) is 6.022E17. This is now internally consistent with the units for the species, RL, and the parameter, kRL.

### Species Initial Amounts

Name	InitialAmount (Molecule)
L	6.022E17
R	10000.0
G	7000.0
Gd	3000.0
Gbg	3000.0

**Species Initial Amounts (Continued)**

Name	InitialAmount (Molecule)
Ga	0.0
RL	0.0

To replicate the published results, the model needs the definition of the ratio of active G protein. Call this ratio `Ga_frac`. `Ga_frac` is  $Ga/Gt$ , where `Ga` is active G protein (Ga-GTP) and `Gt` is the total amount of G protein in a cell. This relationship is defined using a rule, and the procedure to create this rule is described in “Creating a Rule for the G Protein Model” on page 2-25.

Define two additional species, called `Ga_frac` and `Gt`.

**Additional Species**

Name	InitialAmount (Molecule)
<code>Ga_frac</code>	0.0
<code>Gt</code>	10000.0

To add a new species:

- 1** In the **Project Explorer**, click **yeast\_cell Species** to open the **Species** pane.
- 2** In the **Enter name** box, enter the name of a new species, and then click **Add** or press **Enter**.

`Ga_frac`

The species table updates with the new entry and its row is selected. Note that the species is now available in the **Settings** tab.

- 3** In the **Initial Amount** cell, enter a value for the amount of the species. For `Ga_frac`, leave this at the default value (0.0).
- 4** Repeat steps 1 to 3 for `Gt`. **InitialAmount** is 10000.0.



- 5** In the **Settings** tab, select the **ConstantAmount** check box only for Gt, because the amount of Gt does not vary during the simulation.

Your species table should resemble this.

Enter Name: <input type="text"/>					Add	Delete
	Name	Scope	InitialAmount	InitialAmountUnits		
1	L	yeast_cell	6.022E17	<input type="text"/>	<input type="checkbox"/>	
2	R	yeast_cell	10000.0	<input type="text"/>	<input type="checkbox"/>	
3	RL	yeast_cell	0.0	<input type="text"/>	<input type="checkbox"/>	
4	Gd	yeast_cell	3000.0	<input type="text"/>	<input type="checkbox"/>	
5	Gbg	yeast_cell	3000.0	<input type="text"/>	<input type="checkbox"/>	
6	G	yeast_cell	7000.0	<input type="text"/>	<input type="checkbox"/>	
7	Ga	yeast_cell	0.0	<input type="text"/>	<input type="checkbox"/>	
8	Ga_frac	yeast_cell	0.0	<input type="text"/>	<input type="checkbox"/>	—
9	Gt	yeast_cell	10000.0	<input type="text"/>	<input type="checkbox"/>	—

Notice the yellow indicator; move your pointer over the indicator to see the warning message. The message shows that the species is never used, because Ga\_frac and Gt are not yet defined in a rule. After you define the rule as described in the next section, the indicator shows one green square.

For additional help in each procedure, select **Help > SimBiology Desktop Help** for context-sensitive help.

## Creating a Rule for the G Protein Model

A SimBiology rule is a mathematical expression that modifies a species amount, compartment volume, or a parameter value. Use a repeatedAssignment rule to define the value of the species Ga\_frac in the model.

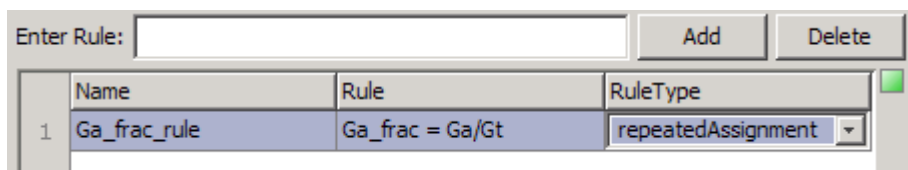
- 1** In the **Project Explorer**, click **Rules** to open the **Rules** pane.
- 2** In the **Enter Rule** box, type the expression, and then click **Add** or press **Enter**.

$Ga\_frac = Ga/Gt$

**3** From the **RuleType** list select `repeatedAssignment`.


**4** (Optional) Give your rule a name. Double-click and type the following in the **Name** box:

`Ga_frac_rule`



This completes the section on building the G protein cycle model for the wild-type strain.

### Verifying the Model

While you are building your model in the SimBiology desktop, you can click  at any time to generate a list of any errors and warnings in the model. The errors and warnings appear in the **Errors and Warnings** pane. For more information about verification see “Verifying that a Model Has No Warnings or Errors” in the SimBiology User’s Guide.

## Simulating the G Protein Cycle Model

### In this section...

“Setting Conditions Before Simulating the G Protein Model” on page 2-27

“Simulation Results for the Wild-Type Strain Model” on page 2-31

### Setting Conditions Before Simulating the G Protein Model

In previous sections, this tutorial described building a model for a G protein cycle. This model uses the G protein cycle in the yeast pheromone response pathway. This section describes conditions for simulation and the simulation results for this model.

Consider the following points about simulating this model:

- Yi. et al. show data up to 600s for the active G protein time course. To replicate these results, change the simulation settings from the default 10 second to 600 second. This change remains active for this model unless you change it back to the default.
- The ligand species 'L' has values that are magnitudes higher than those of many of the other species. Don't log data for 'L' so that while plotting you can enable instant visualization of the other species through proper scaling of plots. To do this, define **Data Logging** to stop logging data for 'L'.

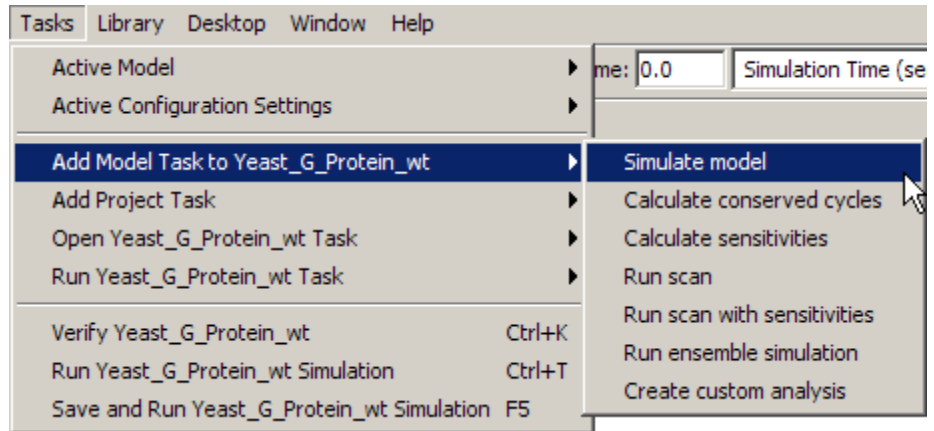
The first procedure (below) describes how to change the simulation stop time. The second procedure is about recording a subset of data (“Specifying Which Data Is Recorded” on page 2-29).

### Adding a Simulation Task

When you created a new project as shown in “Opening the SimBiology Desktop” on page 2-11, the option chosen added a **Simulation** task to the project. You can skip to “Changing the Simulation Stop Time” on page 2-28.

If you have a project without a **Simulation** task, do the following to add a **Simulation** task:

- In the **Task** menu, select **Add Model Task to Yeast\_G\_Protein\_wt > Simulate model**.



The SimBiology desktop adds the task to the **Project Explorer**, opens the task pane, and highlights the new task.

### Changing the Simulation Stop Time

Change the stop time to replicate the simulation used in the reference paper [Yi et al. 2003], and to facilitate comparison with the experimental results presented in the study.

You will modify the default settings for this example. If you do not want to modify the default in your models, you can add another configuration set that you can then modify.

- 1 In the **Project Explorer**, click **Configuration Settings**.
- 2 In the **Settings** tab, enter the stop time in the **Stop** box and press **Enter**.

600.0

Leave the following properties as the default (you may have to scroll to see some of the properties mentioned below):

- **SolverType(sundials)**

- **AbsoluteTolerance** (1.0E-6)
- **RelativeTolerance** (0.0010)
- **MaxStep** (1)
- **DimensionalAnalysis** (check box selected)
- **UnitConversion** (check box clear)
- **DefaultSpeciesDimension** (concentration). This value is important if you are accounting for volume in your model. This example ignores volume and thus the value assigned to this property is not relevant.

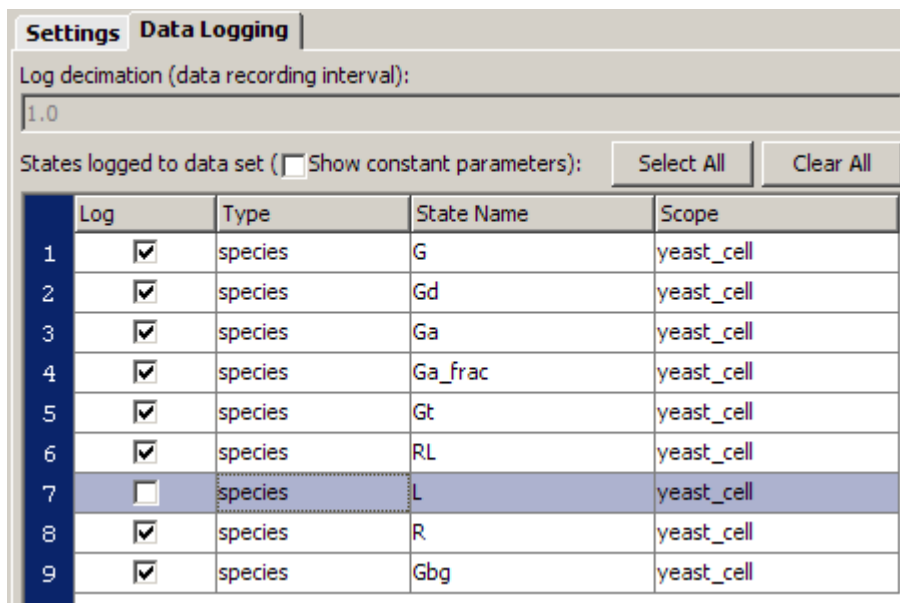
You can also change the solver type to use and the stop time for the simulation in the SimBiology toolbar. The desktop changes the setting of the **Active** configuration set when you change settings in the **Toolbar**.

## Specifying Which Data Is Recorded

You can specify the species names for which SimBiology should *log*, that is, record the simulation data.

As mentioned in the previous section, you will modify the `default` settings for this example. If you do not want to modify the default in your models, you can add another configuration set that you can then modify.

- 1** In the **Configuration Settings** pane, click the **Data Logging** tab.
- 2** Select the check boxes for the species to log. Because, all the species check boxes are selected by default, clear the check box for 'L'. The order of the species in the figure below may not exactly match the order on your screen.



### Tips for Use and Points to Consider

- You can save all these simulation settings as one custom simulation setting. See the context-sensitive help for **Simulation Settings**. To access context-sensitive help, select **Help > SimBiology Desktop Help**.
- The default sundials is adequate for modeling of many biological pathways. You might, however, need a different solver for some models. For more information on choosing solver types, see “Selecting a Solver” in the SimBiology User’s Guide documentation.
- You can choose from three stochastic solvers: `stochastic` (SSA), `implicit tau`, and `explicit tau`. Try one of the stochastic solvers with this model and see how it compares with `sundials`. For information, see “Stochastic Solvers” in the SimBiology User’s Guide documentation. You can also see how the stochastic solvers compare with each other.
- For a counter that tracks the simulation, look in the lower-right corner of the SimBiology desktop.

- Click the following links to learn more about absolute and relative tolerance. These are links to SimBiology reference pages with definitions for `AbsoluteTolerance` and `RelativeTolerance`.

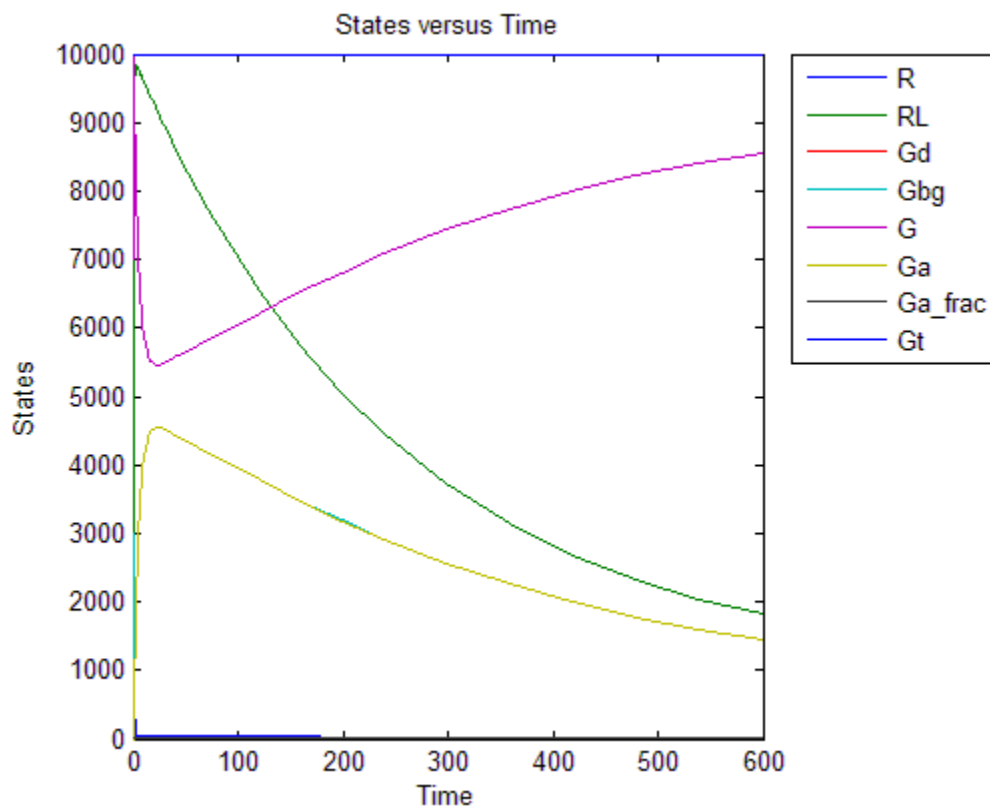
## Simulation Results for the Wild-Type Strain Model

Simulate the model you have built and see your results. To simulate the model:

- 1** In the **Project Explorer**, under **Model Tasks**, click the **Simulation** task to open the **Simulation** pane.

- 2** Click  (**Run**).

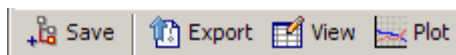
Your plot should resemble the following figure:



### Saving Simulation Data

You can optionally save the data from the most recent simulation run. Unless you save the data for each simulation run, it is overwritten by the data for the next run.

- 1 In the **Project Explorer**, under **Simulation**, click **Data** for the wild-type model.
- 2 In the **Data** pane, click **Save** to open the Save Data dialog box.





**3** Specify a name for your data, and then click **Save**.

```
wt_model_run1
```

The desktop adds the saved data under the **Simulation** task in the **Project Explorer**.

## Creating the Mutant Strain Using a Variant

### In this section...

“Modeling the Mutant Strain” on page 2-34

“Applying Alternate Values Using Variants” on page 2-34

“Simulation Results for the Model of the Mutant Strain” on page 2-35

### Modeling the Mutant Strain

The deletion in SST2 results in uncatalyzed G protein deactivation (Reaction 6;  $Ga \rightarrow Gd$ ). From a modeling perspective, this means a change in the rate of the reaction. This section shows you how represent the value for the mutant strain in a **Variant** and simulate the model using the variant value.

---

**Note** An additional simplifying assumption of this model is that there are no changes in the initial amounts of species or the rate of any other reaction.

---

### Applying Alternate Values Using Variants

- 1 In the **Project Explorer**, click **Variants** to open the **Variants** pane.
- 2 In the **Enter Name** box, type a name for the variant, and then click **Add** or press **Enter**. For example:

```
mut_value
```

- 3 Add content to the variant:
  - a In the **Settings** tab, from the **Type** list, select parameter. The **Property** list updates to show the property available for changing.
  - b Double-click the **Component Name** cell and type the name of the component.

```
Gprotein Inactivation.kGd
```

---

**Tip** Alternatively, double-click the **Component Name** cell, press the down arrow, and select `Gprotein Inactivation.kGd` from the list and press **Enter**.

---

The parameter `kGd` is at the kinetic law level, and not the model level. Thus, you must specify the parameter in the format *ReactionName.ParameterName*.

- c In the **Value** cell, type a value to apply using the variant.


0.004

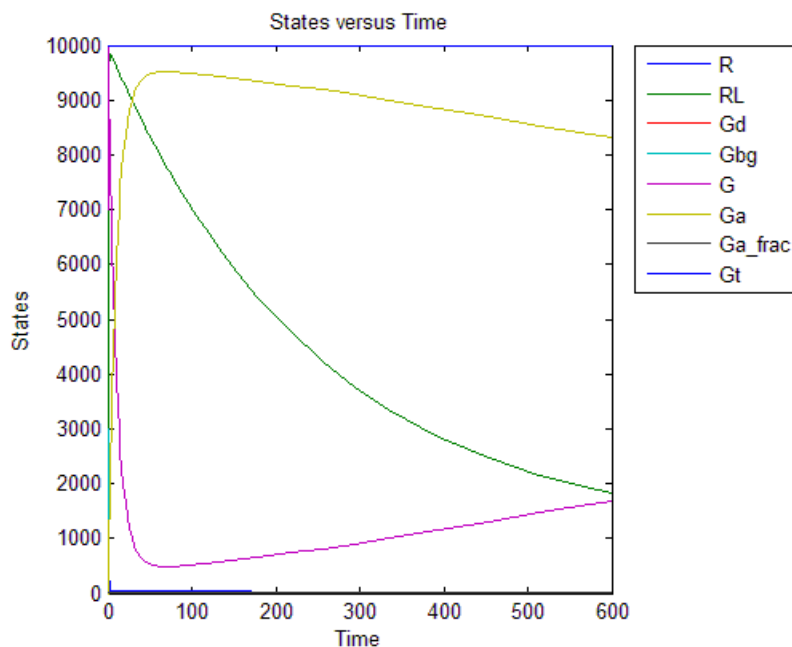
### See Also

“Storing and Applying Alternate Model Values Using Variants” in the *SimBiologyUser’s Guide*.

## Simulation Results for the Model of the Mutant Strain

To simulate the model of the mutant strain, apply the variant and simulate as follows:

- 1 If the **Simulation** pane is not already open, in the **Project Explorer** select **Simulation** to open the pane.
- 2 In the **Variants** table, select the **Use in Task** check box for `mut_value`.
- 3 Click  (**Run**). Your plot should resemble the following figure.



**4** In the **Data** pane for the latest simulation, click **Save** to open the Save Data dialog box.

**5** Specify a name for your data, and then click **Save**.

```
mut_model_run1
```

The desktop adds the saved data under the **Simulation** task in the **Project Explorer**.

The simulation results for the wild-type strain are described in “Simulation Results for the Wild-Type Strain Model” on page 2-31.

## Creating a Custom Plot-Type to View Simulation Results

### In this section...

“Creating a Custom Plot” on page 2-37

“Visualizing Results for the Mutant Strain Using a Custom Plot” on page 2-42

### Creating a Custom Plot

To keep data plots from each model simulation distinct and to facilitate comparison, you can use customized plots. This example shows how to create and save a custom plot in the **Plot Types** library for use in plotting the simulation data with a different line style (dashed lines).

- 1** Select **Library > Show Library Explorer**. The **Library Explorer** opens.
- 2** In the **Library Explorer**, click **Plots Types**. The **Plot Types** pane opens.
- 3** In the **Enter Name** box, type a name for the custom plot and press **Enter**.

Time plot line style

The desktop adds the new plot to the plot types table.

- 4** In the **Enter Plot Type code below or copy Plot Type code from** section, replace the code in the editor window with the following:

```
function Time(tobj, y, lstyle)
%TIME Plots states versus time.
%
% Plot the results of the simulation for the species with the specified
% names versus time. Data from each run is plotted into one axes. The
% string '<all>' can be used to indicate that all species should be
% plotted. LStyle specifies the line style that can be used.
%
% See also GETDATA, SELECTBYNAME.

if (length(tobj) > 1)
    sbioplot(tobj, @timeplotdata, [], y, lstyle);
```

```
else
    timeplotdata(tobj, [], y, lstyle);
end

%-----
function [handles, names] = timeplotdata(tobj, x, y, lstyle)

colors    = get(gca, 'ColorOrder');
numColors = length(colors);
handles = [];
for i=1:length(tobj)
    % Get the data from the next run.
    nexttobj = tobj(i);

    % Get the simulation data associated with the species
    % specified in y.
    if strcmpi(y, '<all>')
        [time, data, names] = getdata(nexttobj);
    else
        [time, data, names] = selectbyname(nexttobj, y);
    end

    % Error checking.
    if size(data,2) == 0
        error('Species specified do not exist.');
```

```
    end

    % Plot data. If there is only one state use different colors for runs.
    if(size(data,2) ==1)
        hLine = plot(time, data, 'color',colors(mod(i-1,numColors)+1,:), 'LineStyle', lstyle);
    else
        hLine = plot(time, data, 'LineStyle', lstyle);
    end
    handles = [handles hLine];
end

% Label.
hold off;
xlabel('Time');
ylabel('States');
```

```
title('States versus Time');  
  
if length(tobj) == 1  
    leg = legend(names, 'Location', 'NorthEastOutside');  
    set(leg, 'Interpreter', 'none');  
end
```

### **Code Modifications for Line Style**

This code uses the `Time` plot type as a starting point and contains the modifications highlighted next.

```

function Time(tobj, y, lstyle)
%TIME Plots states versus time.
%
% Plot the results of the simulation for the species with the specified
% names versus time. Data from each run is plotted into one axes. Use the
% Time Subplot type to plot data from each run into its own subplot. The
% string '<all>' can be used to indicate that all species should be
% plotted. LStyle specifies line style that can be used.
%
% See also GETDATA, SELECTBYNAME.

if (length(tobj) > 1)
    sbiplot(tobj, @timeplotdata, [], y, lstyle);
else
    timeplotdata(tobj, [], y, lstyle);
end

%-----
function [handles, names] = timeplotdata(tobj, x, y, lstyle)

colors = get(gca, 'ColorOrder');
numColors = length(colors);
handles = [];
for i=1:length(tobj)
    % Get the data from the next run.
    nexttobj = tobj(i);

    % Get the simulation data associated with the species
    % specified in y.
    if strcmpi(y, '<all>')
        [time, data, names] = getdata(nexttobj);
    else
        [time, data, names] = selectbyname(nexttobj, y);
    end

    % Error checking.
    if size(data,2) == 0
        error('Species specified do not exist.');
```



- 5 Modify the code to customize the plot type, by typing in the section containing the code. If you change the arguments, the desktop updates the **List of Arguments Passed to Plot Type Code** table with the new list.
- 6 Specify additional information for the `lstyle` argument by double-clicking its row in the table. The Define Argument `lstyle` dialog box opens.
- 7 From the **Define the values that the plot type argument can be configured to** list, select Enumerations. This option lets you specify a comma-separated list of supported values.
- 8 In the **Comma separated list of supported values** box, type the values that can be entered for this plot type. The `Line Style` argument takes the following values:  
  
    `- , -- , - . , : , none`
- 9 From the **Default value of the plot type argument lstyle** list, select a default value. For this example select `--`. This list is populated with the values entered in the **Comma separated list of supported values** box.
- 10 Click **OK** to close the Define Argument `lstyle` dialog box.
- 11 Double click the row containing the `tobj` argument. The Define Argument `tobj` dialog box opens.
- 12 From the **Define the values that the plot type argument can be configured to** list, select `Data Source`.
- 13 Click **OK** to close the Define Argument `tobj` dialog box.
- 14 Double click the row containing the `y` argument. The Define Argument `y` dialog box opens.
- 15 From the **Define the values that the plot type argument can be configured to** list, select `Data Names`, (the `Data Source` for this argument is `tobj`)
- 16 Select the **State Names (what is being logged)** check box. Leave the **Default value of the plot type argument y** as `<all>`.
- 17 Click **OK** to close the Define Argument `y` dialog box.

- 18 Click **Save Now** to save your new plot type. Plot types are automatically saved at regular time intervals. If **Save Now** is disabled, this means that the desktop has automatically saved the plot type.

This plot type is available for use with any task.

### Visualizing Results for the Mutant Strain Using a Custom Plot

Plot the simulation data for the model of the mutant strain with dashed lines. If you have the example open and have simulated the model for the mutant strain you do not need to rerun the simulation. You can use the saved data from “Simulation Results for the Model of the Mutant Strain” on page 2-35. Follow the steps described in “Plotting the Results” on page 2-43.

If you do not have the example open do the following:

- 1 Load the example project by typing the following at the command line:

```
sbioloadproject gprotein
```

The model is stored in a variable called `m1`.

- 2 Open the SimBiology desktop with the model loaded by typing:

```
simbiology(m1)
```

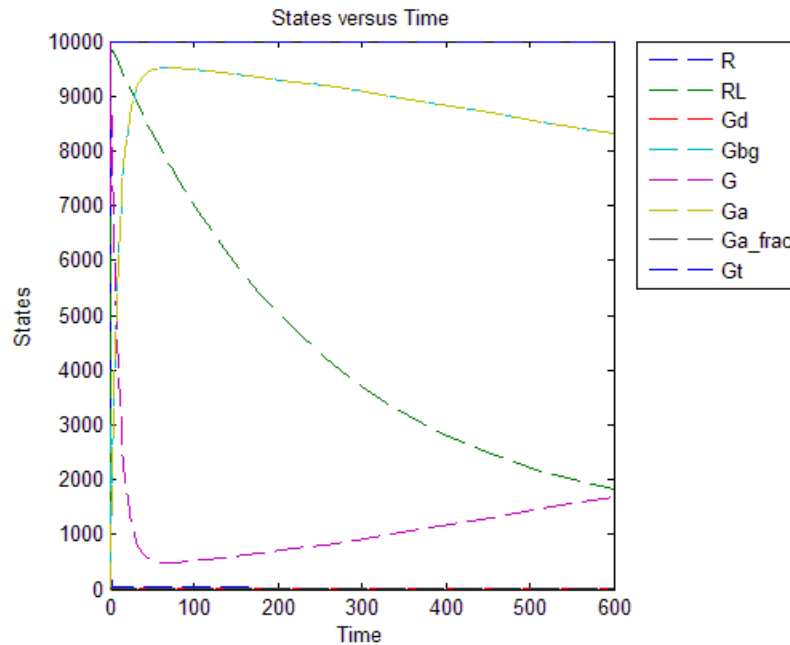
The SimBiology desktop opens with **Model Session-Heterotrimeric\_G\_Protein\_wt**.

- 3 Select **File > Save Project As**. The Save SimBiology Project dialog box opens.
- 4 Specify a name (for example, `gprotein_ex`) and location for your project, and click **Save**.

Simulate the model as shown in “Simulation Results for the Model of the Mutant Strain” on page 2-35, and then continue with the steps described in “Plotting the Results” on page 2-43.

## Plotting the Results

- 1** In the **Project Explorer**, under the **Simulation** task, click `mut_model_run1`.
- 2** In the **Data** pane , click the **Plots** tab.
- 3** From the **Plot Type** list, select Time plot line style and click **Add Plot Type**.
- 4** Under **Arguments**, select `--` from the **lstyle** list.
- 5** In the plot type table, clear the **Create Plot** check box for the Time plot.
- 6** Click **Plot**. Your figure should resemble the following.



## Plotting Species from Two Different Data Sets

### In this section...

“Procedures Described in This Section” on page 2-44

“Plotting the Active G Protein Fraction from the Wild-Type Strain Model” on page 2-44

“Creating a Custom Plot to Compare the Data” on page 2-45

“Plotting the Active G Protein Fraction from the Model of the Mutant Strain” on page 2-46

### Procedures Described in This Section

This section shows you the following:


- How to compare the active G protein fractions in the two simulations. The procedures in this section show you how to create a plot showing species from the two data sets in this tutorial.
- How to plot the data without having to rerun the simulation, and more about how to generate custom plots.

### Plotting the Active G Protein Fraction from the Wild-Type Strain Model

You can find the simulation data under **Simulation** task for the model. You can also save the data from previous simulations. See “Saving Simulation Data” on page 2-32 for more information.

Specify that the species Ga\_frac should be plotted for the wild-type model.

- 1** In the **Project Explorer**, under the **Simulation** task, click wt\_model\_run1. The data saved for the wild-type strain opens.
- 2** In the **Data** pane, click the **Plots** tab.
- 3** From the **Plot Type** list, select the Time plot and click the **Add Plot Type** button.

- 4 In the **Arguments** section, click . The Select Values for y dialog box opens.
- 5 Click **Clear All**.
- 6 Select `yeast_cell.Ga_frac` and click **OK**.
- 7 In the plot type table, clear the **Create Plot** check boxes for the other plots, and click **Plot**. Leave the figure window open.

## Creating a Custom Plot to Compare the Data

Create a custom plot that specifies that the species `Ga_frac` should be plotted with dashed lines for the `sst2Δ` model, and add a legend indicating `Ga_frac` from wild-type (`Ga_frac_wt`) and `Ga_frac` from `sst2Δ` (`Ga_frac_mut`).

- 1 Select **Library > ShowLibrary Explorer**. The **Library Explorer** opens.
- 2 In the **Library Explorer**, click **Plots Types**. The **Plot Types** pane opens.
- 3 In the **Enter Name** box, type a name for the custom plot and press **Enter**.

`Time plot for Ga_frac comparisons`

The desktop adds the new plot to the plot types table.

- 4 In the **Enter Plot Type code below or copy Plot Type code from** section, from the list select `Time plot line style`.
- 5 Click **Apply**. The Plot Types command window updates to show you the code for the `Time plot line style` plot.
- 6 Locate and change the following lines of code:

```
leg = legend(names, 'Location', 'NorthEastOutside');
set(leg, 'Interpreter', 'none');
```

to

```
leg = legend({'Ga_frac_wt', 'Ga_frac_mut'}, 'Location', 'NorthEastOutside');
set(leg, 'Interpreter', 'none');
```


- 7 Click **Save Now**. If **Save Now** is not available (grayed out), this means that the plot type has been automatically saved.

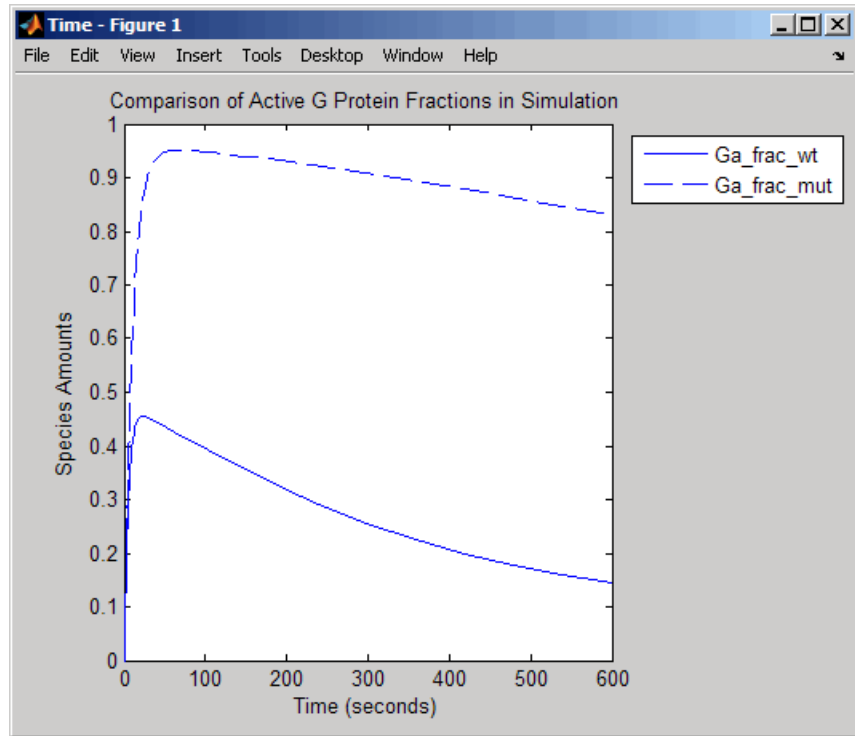
This plot type is available for use with any task for this project.

Now you can plot `Ga_frac` data from the wild-type strain with `Ga_frac` data from the *sst2Δ*.

### Plotting the Active G Protein Fraction from the Model of the Mutant Strain

Plot the *sst2Δ* `Ga_frac` data using dashed lines.

- 1 In the **Project Explorer**, under the **Simulation** task, click `mut_model_run1`
- 2 In the **Data** pane, click the **Plots** tab.
- 3 From the **Plot Type** list, select the Time plot for `Ga_frac` comparisons plot and click **Add Plot Type**.
- 4 In the **Arguments** section, click . The Select Values for y dialog box opens.
- 5 Click **Clear All**.
- 6 Select `yeast_cell.Ga_frac` and click **OK**.
- 7 In the plot type table, clear the **Create Plot** check boxes for the other plots.
- 8 For the newly added plot, from the **Plot Behavior** list, select **Add to current axes** and click **Plot**. This option lets you add data to the most recently generated plot. You must have the figure window open to exercise this option.



## Plotting Experimental Data with Simulation Data

### In this section...

“About the Experimental Data” on page 2-48

“Creating a Custom Plot for Experimental Data” on page 2-48

“Plotting the Data” on page 2-49

### About the Experimental Data

You can work with your experimental data and plot your data from the SimBiology desktop. The section describes how to store the experimental data and use the custom plotting features to plot the data with your simulation data.

This example uses the yeast G protein model built in this tutorial, based on a reference paper published by Yi and colleagues [Yi et al. 2003]. The experimental data used here are also from the same reference paper.

### Creating a Custom Plot for Experimental Data

- 1** Select **Library > Library Explorer**. The **Library Explorer** opens.
- 2** In the **Show Library Explorer**, click **Plots Types**. The **Plot Types** pane opens.
- 3** In the **Enter Name** box, type a name for the custom plot and press **Enter**.

```
Ga_frac Experimental Data Plot
```

The desktop adds the new plot to the plot types table.

- 4** In the **Plot Types** pane, copy and add the following code into the plot types editor window:

```
% 1. Store the time and state data
%(Obtained from Fig. 5 of reference paper.)
x = [0 10 30 60 110 210 300 450 600];
y = [0 0.35 0.4 0.36 0.39 0.33 0.24 0.17 0.2];
```



```

% 2. Store the estimated error values.
%(Obtained from Fig. 5 of reference paper.)
L = [0 0.0100 0 0.0100 0.0200 0.0200 0.0300 0.0200 0.0200];
U = [0 0.0100 0 0.0200 0.0100 0.0180 0.0350 0.0300 0.0100];

% 3. Plot the experimental data.
errorbar(x,y,L,U,'LineStyle','none','Marker','.');
legH3 = legend('Ga_frac_sim','Ga_frac_exp','Location','NorthEastOutside');
set(legH3,'Interpreter','none')

% To make a better picture,
axis([0 600 0 0.5]);

```

### Explanation of the Code

In step 1 you store the data as vectors in two variables, one for the experimental values of active G protein fractions ( $x$ ), and the other for the time points ( $y$ ). By writing scripts in this command window, you can store and process your experimental data before plotting.

In step 2 you store the estimated upper ( $U$ ) and lower ( $L$ ) bounds of the error values of each data point.

In step 3, the function `errorbar` enables you to plot  $x$  versus  $y$  with error bars  $L(i)+U(i)$  long.  $x$ ,  $y$ ,  $L$ , and  $U$  must be the same size. When they are vectors, each error bar is a distance of  $L(i)$  below and  $U(i)$  above the point defined by  $(x(i),y(i))$ . For more information, see `errorbar`.

The code also specifies legend location, marker style, line style, and axis scale. For more information, see `legend` and `axis`.

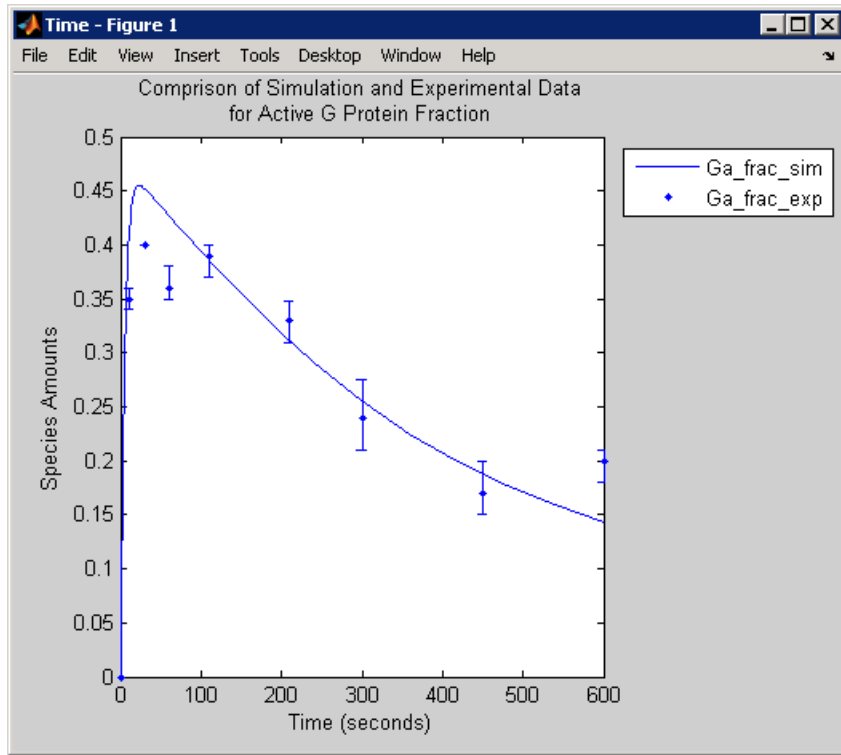
- 5 Click **Save Now**. If **Save Now** is not available (grayed out), this means that the plot type has been automatically saved.

This plot type is available for use with any task for this project.

### Plotting the Data

You can add the new custom plot to the data plot for the model of the wild-type strain and plot the simulation data for `Ga_frac` with the experimental data.

- 1** In the **Project Explorer**, click **Data** for the wild-type model (.wt\_model\_run1)
- 2** In the **Data** pane, click the **Plots** tab.
- 3** From the **Plot Type** list, select the Ga\_frac Experimental Data Plot plot and click **Add Plot Type**.
- 4** Select the **Create Plot** check box for the following:
  - a** For the Time plot in which only Ga is specified in the **Y Arguments** list, select New Figure from the **Plot Behavior** list.
  - b** For the Ga\_frac Experimental Data Plot, select Add to current axes from the **Plot Behavior** list.
- 5** In the plot type table, clear the **Create Plot** check boxes for the other plots and click **Plot**.



For more information on the plot used in step 4a, see “Plotting the Active G Protein Fraction from the Wild-Type Strain Model” on page 2-44.

## References

- [1] Tau-Mu Yi, Hiroaki Kitano, and Melvin I. Simon. A quantitative characterization of the yeast heterotrimeric G protein cycle. PNAS (2003) vol. 100, 10764-10769.
- [2] Alberts, B., Bray, D., Lewis, J., Raff, M., Roberts, K., and Watson, J.D. Molecular Biology of the Cell, 3rd edition, Garland Publishing, 1994.

# M-Phase Control in *Xenopus* Oocyte Extracts

---

John Tyson's Computational Cell Biology Lab created a mathematical model for M-phase control in *Xenopus* oocyte (frog egg) extracts [Marlovits et al. 1998]. The M-phase control model shows principles by which you can apply phosphorylation and regulatory loops in your own models. Publications typically list systems of ordinary differential equations (ODEs) that represent a model system. This example shows you how to interpret these ODEs in the form of reaction pathways that are easier to represent and visualize in SimBiology software.

The model is centered around M-phase promoting factor (MPF). There are two positive feedback loops where MPF increases its synthesis and a negative feedback loop where MPF decreases its amount by increasing its degradation.

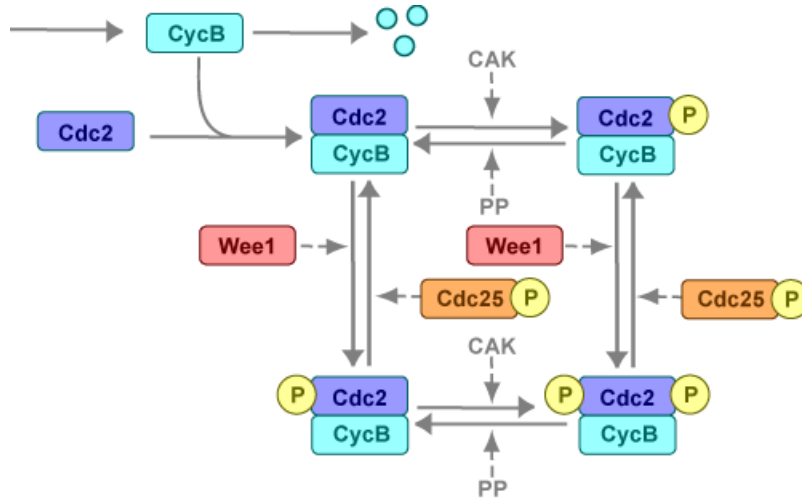
- “M-Phase Control Model” on page 3-2
- “M-Phase Control Equations” on page 3-4
- “SimBiology Model with Rate and Algebraic Rules” on page 3-13
- “SimBiology Model with Reactions and Algebraic Rules” on page 3-21
- “References” on page 3-39

## M-Phase Control Model

In this section...
“Synthesis Reactions” on page 3-2
“Regulation Reactions with Active MPF” on page 3-2

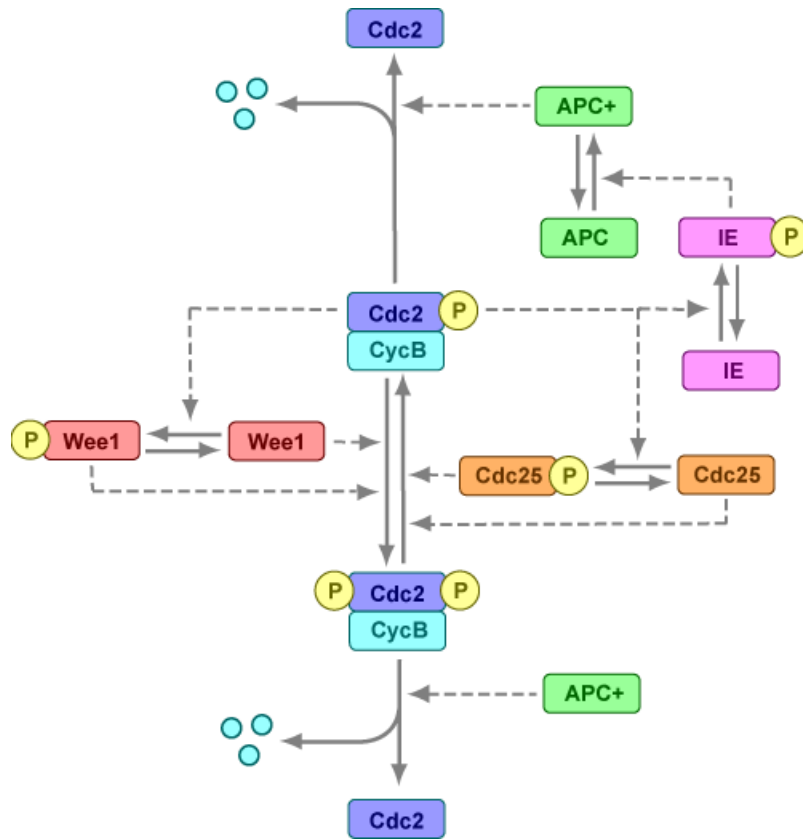
### Synthesis Reactions

Cyclin B (CycB) dimerizes with Cdc2 kinase (Cdc2) to form M-phase promoting factor (MPF).



### Regulation Reactions with Active MPF

Positive feedback loops with M-phase promoting factor (MPF) activate the Cdc25 phosphatase and deactivate the Wee1 kinase. A negative feedback loop with MPF activates anaphase-promoting complex (APC) that regulates the degradation of the Cyclin B subunit.



## M-Phase Control Equations

### In this section...

“About the Rate Equations in This Example” on page 3-4

“Converting Differential Equations to Reactions” on page 3-4

“Equation 1, Cyclin B” on page 3-6

“Equation 2, M-Phase Promoting Factor” on page 3-6

“Equation 3, Inhibited M-Phase Promoting Factor” on page 3-7

“Equation 4, Inhibited and Activated M-Phase Promoting Factor” on page 3-8

“Equation 5, Activated M-Phase Promoting Factor” on page 3-8

“Equation 11, Cell Division Control 25” on page 3-9

“Equation 12, Wee1 Activation/Deactivation” on page 3-10

“Equation 13, Intermediate Enzyme Activation/Deactivation” on page 3-10

“Equation 14, APC Activation/Deactivation” on page 3-11

“Equation 17, Rate Parameter K2” on page 3-11

“Equation 18, Rate Parameter Kcdc25” on page 3-12

“Equation 19, Rate Parameter Kwee1” on page 3-12

### About the Rate Equations in This Example

Models in systems biology are commonly described in the literature with differential rate equations. However, SimBiology software defines a model using reactions. This section shows you how to convert models published in the literature to a SimBiology format. The equation numbers match the published paper for this model [Marlovits et al. 1998]. Equations that are missing in the sequence involve the Cdk inhibitor (CKI) protein, which is not currently modeled in the SimBiology version.

### Converting Differential Equations to Reactions

The rules for writing reaction and reaction rate equations from differential rate equations include not only the equations but also an understanding of



the reactions.  $dx/dt$  refers to the species the differential rate equation is defining. *kinetics* refers to the species in the reaction rate.

- Positive terms: Rate species are placed on right side of the reactions; reaction rate equation species are placed on the left.

$$\text{kinetics} \rightarrow \frac{dx}{dt}$$

- Negative terms: Rate species are placed on the left side of the reaction because the species are being used up in some way; reaction rate equation species are also placed on left. You need to deduce the products from additional information about the model.

$$\text{kinetics or } \left(\frac{dx}{dt}\right) \rightarrow \text{products?}$$

The following table will help you deduce the products for a reaction. In this example, by convention, phosphate groups on the right side of a species name are activating while phosphate groups on left are inhibiting.

Enzyme	Description	Reaction
wee1	Kinase, add inhibiting phosphate group	MPF $\rightarrow$ P-MPF
cdc25	Phosphatase, remove inhibiting phosphate group	P-MPF $\rightarrow$ MPF + P
kcaK	Kinase, add activating phosphate group	MPF $\rightarrow$ MPF <sub>p</sub>
kpp	Phosphatase, remove activating phosphate group	MPF-P $\rightarrow$ MPF + P
MPF	Kinase, add activating or inhibiting phosphate group	Wee1/Cdc25/IE $\rightarrow$ X-P or P-X
ki	Add inhibiting Cki	Cki + MPF $\rightarrow$ Cki:MPF
kir	Remove inhibiting Cki	Cki:MPF $\rightarrow$ Cki + MPF

## Equation 1, Cyclin B

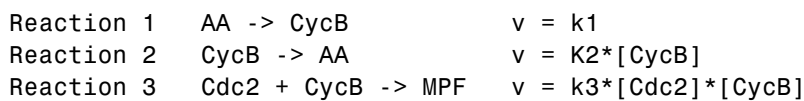
Differential rate equation for cyclin B [Marlovits et al. 1998].

$$\frac{d[\text{CycB}]}{dt} = +k_1 - k_2[\text{CycB}] - k_3[\text{Cdc2}][\text{CycB}]$$

Rate rule using SimBiology format for the differential rate equation 1. For a model using this rule, see “SimBiology Model with Rate and Algebraic Rules” on page 3-13.

$$\text{Rule 1 } [\text{CycB}] = k_1 - K_2 * [\text{CycB}] - k_3 * [\text{Cdc2}] * [\text{CycB}]$$

Reaction and reaction rate equations derived from the differential rate equation. For a model using these reactions, see “SimBiology Model with Reactions and Algebraic Rules” on page 3-21.



## Equation 2, M-Phase Promoting Factor

Differential rate equation for M-phase promoting factor (MPF) [Marlovits 1998]. Note that the parameter name kcakr [Marlovits et al. 1998] is changed to kpp [Borisuk 1998] in the following reaction equations. MPF is a heterodimer of cdc2 kinase and cyclin B.

$$\begin{aligned} \frac{d[\text{MPF}]}{dt} = & +k_3[\text{Cdc2}][\text{CycB}] - K_2[\text{MPF}] \\ & +k_{pp}[\text{MPF}_p] - k_{cak}[\text{MPF}] \\ & +K_{cdc25}[\text{pMPF}] - K_{wee1}[\text{MPF}] \\ & +k_{ir}[\text{Cki:MPF}] - k_{i}[\text{MPF}][\text{Cki}] \end{aligned}$$

Rate rule using SimBiology format for the differential rate equation 1. For a model using this rule, see “SimBiology Model with Rate and Algebraic Rules” on page 3-13.

$$\text{Rule 2 MPF} = k_{pp} * \text{MPF}_p - (K_{wee1} + k_{cak} + K_2) * \text{MPF} + K_{cdc25} * \text{pMPF} + k_3 * \text{Cdc2} * \text{CycB}$$

Reaction and reaction rate equations derived from the differential rate equation. For a model using these reactions, see “SimBiology Model with Reactions and Algebraic Rules” on page 3-21. A reaction name in parentheses denotes a reaction repeated in another differential rate equation.

(Reaction 3)	Cdc2 + CycB -> MPF	v = k3*[Cdc2]*[CycB]
Reaction 4	MPF -> Cdc2 + AA	v = K2*[MPF]
Reaction 5	MPFp -> MPF	v = kpp*[MPFp]
Reaction 6	MPF -> MPFp	v = kcak*[MPF]
Reaction 7	pMPF -> MPF	v = Kcdc25*[pMPF]
Reaction 8	MPF -> pMPF	v = Kwee1*[MPF]

### Equation 3, Inhibited M-Phase Promoting Factor

Differential rate equation for inhibited M-phase promoting factor (pMPF) [Marlovits 1998].

$$\frac{d[\text{pMPF}]}{dt} = -K2[\text{pMPF}] + kpp[\text{pMPFp}] - kcak[\text{pMPF}] + Kwee1[\text{MPF}] - Kcdc25[\text{pMPF}] + kd[\text{Cki:pMPF}]$$

Rate rule using SimBiology format for the differential rate equation 3. For a model using this rule, see “SimBiology Model with Rate and Algebraic Rules” on page 3-13.

```
Rule 3 pMPF = Kwee1*MPF - (Kcdc25 + kcak +
K2)*pMPF + kpp*pMPFp
```

Reaction and reaction rate equations derived from the differential rate equation. For a model using these reactions, see “SimBiology Model with Reactions and Algebraic Rules” on page 3-21.

Reaction 11	pMPF -> Cdc2 + AA	v = K2*[pMPF]
Reaction 12	pMPFp -> pMPF	v = kpp*[pMPFp]
Reaction 13	pMPF -> pMPFp	v = kcak*[pMPF]
(Reaction 8)	MPF -> pMPF	v = Kwee1*[MPF]
(Reaction 7)	pMPF -> MPF	v = Kcdc25*[pMPF]

### Equation 4, Inhibited and Activated M-Phase Promoting Factor

Differential rate equation for inhibited and activated M-phase promoting factor (pMPFp) [Marlovits 1998].

$$\begin{aligned} \frac{d[\text{pMPFp}]}{dt} = & -K2[\text{pMPFp}] \\ & +kcak[\text{pMPF}] -kpp[\text{pMPFp}] \\ & +Kwee1[\text{MPFp}] -Kcdc25[\text{pMPFp}] \\ & +kd[\text{Cki:pMPFp}] \end{aligned}$$

Rate rule using SimBiology format for the differential rate equation. For a model using this rule, see “SimBiology Model with Rate and Algebraic Rules” on page 3-13.

```
Rule 4 pMPFp = Kwee1*MPFp - (kpp + Kcdc25 + K2)*pMPFp
+ kacak*pMPF
```

Reaction and reaction rate equations derived from the differential rate equation. For a model using these reactions, see “SimBiology Model with Reactions and Algebraic Rules” on page 3-21.

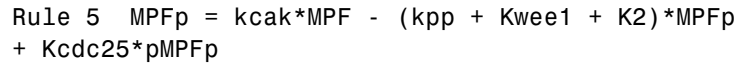
```
Reaction 15  pMPFp -> Cdc2 + AA      v = K2*[pMPFp]
(Reaction 13) pMPF -> pMPFp          v = kacak*[pMPF]
(Reaction 12) pMPFp -> pMPF          v = kpp*[pMPFp]
Reaction 16  MPFp -> pMPFp           v = Kwee1*[MPFp]
Reaction 17  pMPFp -> MPFp           v = Kcdc25*[pMPFp]
```

### Equation 5, Activated M-Phase Promoting Factor

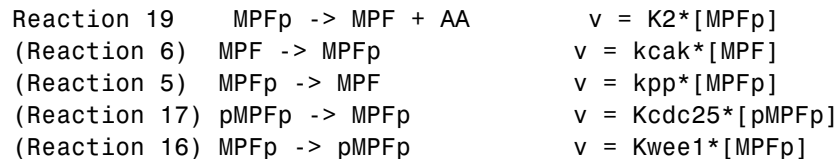
Differential rate equation for activated M-phase promoting factor (MPFp) [Marlovits 1998].

$$\begin{aligned} \frac{d[\text{MPFp}]}{dt} = & -K2[\text{MPFp}] \\ & +kcak[\text{MPF}] -kpp[\text{MPFp}] \\ & +Kcdc25[\text{pMPFp}] -Kwee1[\text{MPFp}] \\ & +kir[\text{CKI:MPFp}] -ki[\text{CKI}][\text{MPFp}] \end{aligned}$$

Rate rule using SimBiology format for the differential rate equation 1. For a model using this rule, see “SimBiology Model with Rate and Algebraic Rules” on page 3-13.



Reaction and reaction rate equations derived from the differential rate equation. For a model using these reactions, see “SimBiology Model with Reactions and Algebraic Rules” on page 3-21.

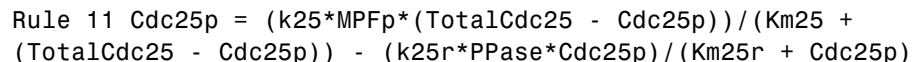


## Equation 11, Cell Division Control 25

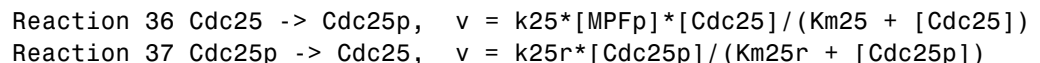
Differential rate equation for activating and deactivating Cdc25 [Marlovits 1998].

$$\frac{d[\text{Cdc25p}]}{dt} = + \frac{k_{25}[\text{MPFp}][\text{Cdc25}]}{K_{m25} + [\text{Cdc25}]} - \frac{k_{25r}[\text{Cdc25p}]}{K_{m25r} + [\text{Cdc25p}]}$$

Rate rule in SimBiology format for the differential rate equation 1. For a model using this rule, see “SimBiology Model with Rate and Algebraic Rules” on page 3-13. Note that since there isn’t a rate rule for Cdc25, its amount is written as (TotalCdc25 - Cdc25p).



Reaction and reaction rate equations derived from the differential rate equation. For a model using these reactions, see “SimBiology Model with Reactions and Algebraic Rules” on page 3-21.



## Equation 12, Wee1 Activation/Deactivation

Differential rate equation for activating and deactivating Wee1 kinase [Marlovits 1998]. The kinase (MPFp) phosphorylates active Wee1 (Wee1) to its inactive form (Wee1p). The dephosphorylation of inactive Wee1 (Wee1p) is by an unknown phosphatase.

$$\frac{d[Wee1]}{dt} = -\frac{k_w[MPFp][Wee1]}{K_{mw} + [Wee1]} + \frac{k_{wr}[Wee1P]}{K_{mwr} + [Wee1P]}$$

Rate rule in SimBiology format for the differential rate equation 1. For a model using this rule, see “SimBiology Model with Rate and Algebraic Rules” on page 3-13.

```
Rule 12 Wee1p = (kw*MPFp*(TotalWee1 - Wee1p))/(Kmw + (TotalWee1 - Wee1p))
              - (kwr*Wee1p)/(Kmwr + Wee1p)
```

Reaction and reaction rate equations derived from the differential rate equation. For a model using these reactions, see “SimBiology Model with Reactions and Algebraic Rules” on page 3-21.

```
reaction 38 Wee1 -> Wee1p, v = (kw*[MPFp]*[Wee1])/(Kmw + [Wee1])
reaction 39 Wee1p -> Wee1, v = (kwr*[Wee1p])/(Kmwr + [Wee1p])
```

## Equation 13, Intermediate Enzyme Activation/Deactivation

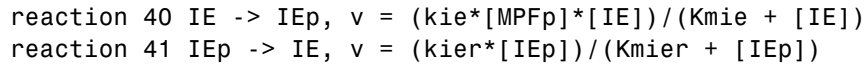
Differential rate equation for activating and deactivating the intermediate enzyme (IE) [Marlovits 1998]. The active kinase (MPFp) phosphorylates the inactive intermediate enzyme (IE) to its active form (IEp).

$$\frac{d[IEp]}{dt} = +\frac{k_{ie}[MPFp][IE]}{K_{mie} + [IE]} - \frac{k_{ier}[IEp]}{K_{mier} + [IEp]}$$

Rate rule in SimBiology format for the differential rate equation 1. For a model using this rule, see “SimBiology Model with Rate and Algebraic Rules” on page 3-13.

```
Rule 13 IEp = (kie*MPFp*(TotalIE - IEp))/(Kmie + (TotalIE - IEp))
              - (kier*IEp)/(Kmier + IEp)
```

Reaction and reaction rate equations derived from the differential rate equation. For a model using these reactions, see “SimBiology Model with Reactions and Algebraic Rules” on page 3-21.

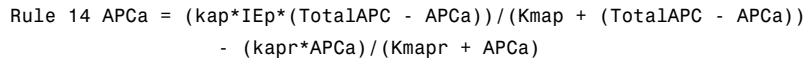


## Equation 14, APC Activation/Deactivation

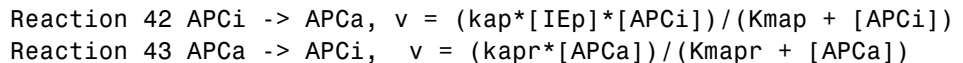
Differential rate equation for [Marlovits 1998].

$$\frac{d[APCa]}{dt} = + \frac{kap[IEP][APCi]}{Kmap + [APCi]} - \frac{kapr[APCa]}{Kmapr + [APCa]}$$

Rate rule in SimBiology format for the differential rate equation 1. For a model using this rule, see “SimBiology Model with Rate and Algebraic Rules” on page 3-13.



Reaction and reaction rate equations derived from the differential rate equation. For a model using these reactions, see “SimBiology Model with Reactions and Algebraic Rules” on page 3-21.

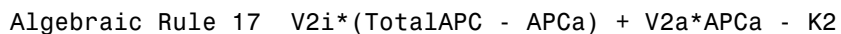


## Equation 17, Rate Parameter K2

Algebraic equation to define the rate parameter K2 [Marlovits 1998]. Inactive APC (APCi) is catalyzed by IE (intermediate enzyme) to active APC (APCa).

$$k2 = V2'[APC] + V2''[APC']$$

Algebraic rule in SimBiology format for the algebraic equation 17. For a model using this rule, see “SimBiology Model with Rate and Algebraic Rules” on page 3-13.



Algebraic rule when simulating with reactions. For a model using this rule with reactions, see “SimBiology Model with Reactions and Algebraic Rules”

on page 3-21. V2' is renamed to V2i and V2 is renamed to V2a. APCi (APC) is the inactive form of the enzyme while APCa (APC') is the active form. K2 is the independent variable.

$$\text{Algebraic Rule 1 } (V2i*APCi) + (V2a*APCa) - K2$$

### **Equation 18, Rate Parameter Kcdc25**

Algebraic equation to define the rate parameter Kcdc25 [Marlovits 1998]. Inactive Cdc25 (Cdc25) is phosphorylated by MPF to active Cdc25 (Cdc25p).

$$kcdc25 = V25'[Cdc25] + V25''[Cdc25p]$$

Algebraic rule in SimBiology format for the algebraic equation 18. For a model using this rule, see “SimBiology Model with Rate and Algebraic Rules” on page 3-13.

$$\text{Algebraic Rule 18 } V25i*(TotalCdc25 - Cdc25p) + V25a*Cdc25p - Kcdc25$$

Algebraic rule when simulating with reactions. Kcdc25 is the independent variable. For a model using this rule with reactions, see “SimBiology Model with Reactions and Algebraic Rules” on page 3-21.

$$\text{Algebraic Rule 2 } (V25i*Cdc25) + (V25a*Cdc25p) - Kcdc25$$

### **Equation 19, Rate Parameter Kwee1**

Algebraic equation to define the rate parameter [Marlovits 1998]. Active Wee1 (Wee1) is phosphorylated by MPF to inactive Wee1 (Wee1p).

$$kwee1 = Vwee1'[Wee1p] + Vwee1''[Wee1]$$

Algebraic rule in SimBiology format for rate parameter equation 19. For a model using this rule, see “SimBiology Model with Rate and Algebraic Rules” on page 3-13.

$$\text{Algebraic Rule 19 } Vwee1i*Wee1p + Vwee1a*(TotalWee1 - Wee1p) - Kwee1$$

Algebraic rule when simulating with reactions. Kwee1 is the independent variable. For a model using this rule with reactions, see “SimBiology Model with Reactions and Algebraic Rules” on page 3-21.

$$\text{Algebraic Rule 3 } (Vwee1i*Wee1p) + (Vwee1a*Wee1) - Kwee1$$



## SimBiology Model with Rate and Algebraic Rules

### In this section...

“Overview” on page 3-13

“Writing Differential Rate Equations as Rate Rules” on page 3-14

“Species” on page 3-14

“Parameters” on page 3-15

“Rate Rule 1, Cyclin B (CycB)” on page 3-16

“Rate Rule 2, M-Phase Promoting Factor (MPF)” on page 3-17

“Rate Rule 3, Inhibited M-Phase Promoting Factor (pMPF)” on page 3-17

“Rate Rule 4, Activated but Inhibited M-Phase Promoting Factor (pMPFp)” on page 3-18

“Rate Rule 5, Activated M-Phase Promoting Factor (MPFp)” on page 3-18

“Rate Rule 11, Activated Cdc25 (Cdc25p)” on page 3-18

“Rate Rule 12, Inhibited Wee1 (Wee1p)” on page 3-18

“Rate Rule 13, Activated Intermediate Enzyme (IEp)” on page 3-18

“Rate Rule 14, Activated APC (APCa)” on page 3-18

“Algebraic Rule 17, Rate Parameter K2” on page 3-19

“Algebraic Rule 18, Rate Parameter Kcdc25” on page 3-19

“Algebraic Rule 19, Rate Parameter Kwee1” on page 3-19

“Simulation of the M-Phase Control Model with Rules” on page 3-19

### Overview

There is one rate rule for each equation defining a species and one algebraic rule for each variable parameter in the M-phase control model [Marlovits 1998]. For a list and description of the equations, see “M-Phase Control Equations” on page 3-4.

A basic model includes rate rules 1 to 5 and 11 to 14 with algebraic rules 17, 18, and 19.

## Writing Differential Rate Equations as Rate Rules

Writing differential rate equations in an unambiguous format that a software program can understand is a simple process when you follow the syntax rules for programming languages.

- Use an asterisk to indicate multiplication. For example,  $k[A]$  is written  $k*A$  or  $k*[A]$ . The brackets around the species A do not indicate concentration.
- SimBiology uses square brackets around species and parameter name to allow names that are not valid MATLAB variable names. For example, you could have a species named `glucose-6-phosphate dehydrogenase` but you need to add brackets around the name in reaction rate and rule equations.

`[glucose-6-phosphate dehydrogenase]`

- Use parentheses to clarify the order of evaluation for mathematical operations. For example, do not write Henri-Michaelis-Menten reaction rates as  $V_m*C/K_d + C$ , because  $V_m*C$  is divided by  $K_d$  before adding  $C$  to the result. Instead, write this reaction rate as  $(V_m*C)/(K_d + C)$ .

## Species

The following table lists species in the model with their initial amounts. There are three variable parameters modeled as species (`K2`, `Kcdc25`, and `KWee1`). You could also model the variable parameters as parameters with the property **ConstantAmount** cleared.

Name	InitialAmount ▲	InitialAmountUnits	ConstantAmount
CycB	0.0		<input type="checkbox"/>
MPF	0.0		<input type="checkbox"/>
pMPF	0.0		<input type="checkbox"/>
pMPFp	0.0		<input type="checkbox"/>
MPFp	0.0		<input type="checkbox"/>
Cdc25p	0.0		<input type="checkbox"/>
Wee1p	0.0		<input type="checkbox"/>
IEp	0.0		<input type="checkbox"/>
APCa	0.0		<input type="checkbox"/>
Kcdc25	0.0		<input type="checkbox"/>
Kwee1	0.0		<input type="checkbox"/>
K2	0.0		<input type="checkbox"/>
Wee1	0.0		<input type="checkbox"/>
TotalCdc25	1.0		<input checked="" type="checkbox"/>
TotalWee1	1.0		<input checked="" type="checkbox"/>
TotalAPC	1.0		<input checked="" type="checkbox"/>
TotalIE	1.0		<input type="checkbox"/>
PPase	1.0		<input checked="" type="checkbox"/>
AntiAPC	1.0		<input checked="" type="checkbox"/>
Cdc2	100.0		<input checked="" type="checkbox"/>

## Parameters

The following table lists parameters in the model with their initial values. The property **ConstantValue** is selected for all of the parameters.

Name	Value ▾	ValueUnits	ConstantValue
Vweea	1.0		<input checked="" type="checkbox"/>
k1	1.0		<input checked="" type="checkbox"/>
Kmwr	1.0		<input checked="" type="checkbox"/>
Kmapr	1.0		<input checked="" type="checkbox"/>
Km25r	1.0		<input checked="" type="checkbox"/>
kcak	0.64		<input checked="" type="checkbox"/>
V2a	0.25		<input checked="" type="checkbox"/>
V25a	0.17		<input checked="" type="checkbox"/>
kier	0.15		<input checked="" type="checkbox"/>
kapr	0.13		<input checked="" type="checkbox"/>
kap	0.13		<input checked="" type="checkbox"/>
kwr	0.1		<input checked="" type="checkbox"/>
k25r	0.1		<input checked="" type="checkbox"/>
Kmw	0.1		<input checked="" type="checkbox"/>
Km25	0.1		<input checked="" type="checkbox"/>
kie	0.02		<input checked="" type="checkbox"/>
kw	0.02		<input checked="" type="checkbox"/>
k25	0.02		<input checked="" type="checkbox"/>
V25i	0.017		<input checked="" type="checkbox"/>
Vweei	0.01		<input checked="" type="checkbox"/>
Kmier	0.01		<input checked="" type="checkbox"/>
Kmie	0.01		<input checked="" type="checkbox"/>
Kmap	0.01		<input checked="" type="checkbox"/>
V2i	0.0050		<input checked="" type="checkbox"/>
k3	0.0050		<input checked="" type="checkbox"/>
kpp	0.0040		<input checked="" type="checkbox"/>

### Rate Rule 1, Cyclin B (CycB)

The rate rule is from “Equation 1, Cyclin B” on page 3-6.

$$\text{rate rule: CycB} = k1 - K2*\text{CycB} - k3*\text{Cdc2}*\text{CycB}$$

```

species: CycB = 0 nM
         Cdc2 = 100 nM, [x]constant
parameters: k1 = 1 nM/minute
            K2 = 0 1/minute, []constant
            k3 = 0.005 1/(nM*minute)
    
```

K2 is a variable rate parameter whose value is defined by an algebraic rule. See “Algebraic Rule 17, Rate Parameter K2” on page 3-19. Its value varies from 0.005 to 0.25 1/minute.

## Rate Rule 2, M-Phase Promoting Factor (MPF)

The rate rule is from “Equation 2, M-Phase Promoting Factor” on page 3-6.

```

rate rule: MPF = kpp*MPFp - (Kwee1 + kcak + K2)*MPF + Kcdc25*pMPF
           + k3*Cdc2*CycB
species: MPF = 0 nM
         MPFp = 0 nM
         pMPF = 0 nM
parameters: kpp = 0.004 1/minute
            kcak = 0.64 1/minute
            k3 = 0.005 1/(nM*minute)
            K2 = 0 1/minute
            Kcdc25 = 0 1/minute
            Kwee1 = 0 1/minute
    
```

K2, Kcdc25, and Kwee1 are variable rate parameters whose values are defined by algebraic rules. See “Algebraic Rule 17, Rate Parameter K2” on page 3-19, “Algebraic Rule 18, Rate Parameter Kcdc25” on page 3-19, and “Algebraic Rule 19, Rate Parameter Kwee1” on page 3-19.

## Rate Rule 3, Inhibited M-Phase Promoting Factor (pMPF)

The rate rule is from “Equation 3, Inhibited M-Phase Promoting Factor” on page 3-7.

```

rate rule: pMPF = Kwee1*MPF - (Kcdc25 + kcak + K2)*pMPF + kpp*pMPFp
    
```

### **Rate Rule 4, Activated but Inhibited M-Phase Promoting Factor (pMPFp)**

The rate rule is from “Equation 4, Inhibited and Activated M-Phase Promoting Factor” on page 3-8.

$$\text{rate rule: pMPFp} = K_{wee1} * MPFp - (k_{pp} + K_{cdc25} + K_2) * pMPFp + k_{cak} * pMPF$$

### **Rate Rule 5, Activated M-Phase Promoting Factor (MPFp)**

The rate rule is from “Equation 5, Activated M-Phase Promoting Factor” on page 3-8.

$$\text{rate rule: MPFp} = k_{cak} * MPF - (k_{pp} + K_{wee1} + K_2) * MPFp + K_{cdc25} * pMPFp$$

### **Rate Rule 11, Activated Cdc25 (Cdc25p)**

The rate rule is from “Equation 11, Cell Division Control 25” on page 3-9.

$$\begin{aligned} \text{rate rule: Cdc25p} = & (k_{25} * MPFp * (TotalCdc25 - Cdc25p)) / (K_{m25} + (TotalCdc25 - Cdc25p)) \\ & - (k_{25r} * PPase * Cdc25p) / (K_{m25r} + Cdc25p) \end{aligned}$$

### **Rate Rule 12, Inhibited Wee1 (Wee1p)**

The rate rule is from “Equation 12, Wee1 Activation/Deactivation” on page 3-10.

$$\begin{aligned} \text{rate rule: Wee1p} = & (k_w * MPFp * (TotalWee1 - Wee1p)) / (K_{mw} + (TotalWee1 - Wee1p)) \\ & - (k_{wr} * PPase * Wee1p) / (K_{mwr} + Wee1p) \end{aligned}$$

### **Rate Rule 13, Activated Intermediate Enzyme (IEp)**

The rate rule is from “Equation 13, Intermediate Enzyme Activation/Deactivation” on page 3-10.

$$\begin{aligned} \text{rate rule: IEp} = & (k_{ie} * MPFp * (TotalIE - IEp)) / (K_{mie} + (TotalIE - IEp)) \\ & - (k_{ier} * PPase * IEp) / (K_{mier} + IEp) \end{aligned}$$

### **Rate Rule 14, Activated APC (APCa)**

The rate rule is from “Equation 14, APC Activation/Deactivation” on page 3-11.

```
rate rule: APCa = (kap*IEp*(TotalAPC - APCa))/(Kmap + (TotalAPC - APCa))
            - (kapr*AntiAPC*APCa)/(Kmapr + APCa)
```

## Algebraic Rule 17, Rate Parameter K2

K2 is a variable rate parameter whose value is determined by the amount of active and inactive APC. The algebraic rule is from “Equation 17, Rate Parameter K2” on page 3-11.

```
algebraic rule: V2i*(TotalAPC - APCa) + V2a*APCa - K2
species: APCi = 1 nM
          APCa = 0 nM
          TotalAPC = 1 nM [x]constant
parameters: K2 = 0 or 0.25 1/minute, []constant
            V2i = 0.005 1/(nM*minute)
            V2a = 0.25 1/(nM*minute)
```

## Algebraic Rule 18, Rate Parameter Kcdc25

Kcdc25 is a variable rate parameter whose value is determined by the amount of active and inactive Cdc25. The algebraic rule is from “Algebraic Rule 18, Rate Parameter Kcdc25” on page 3-19.

```
algebraic rule: V25i*(TotalCdc25 - Cdc25p) + V25a*Cdc25p - Kcdc25
```

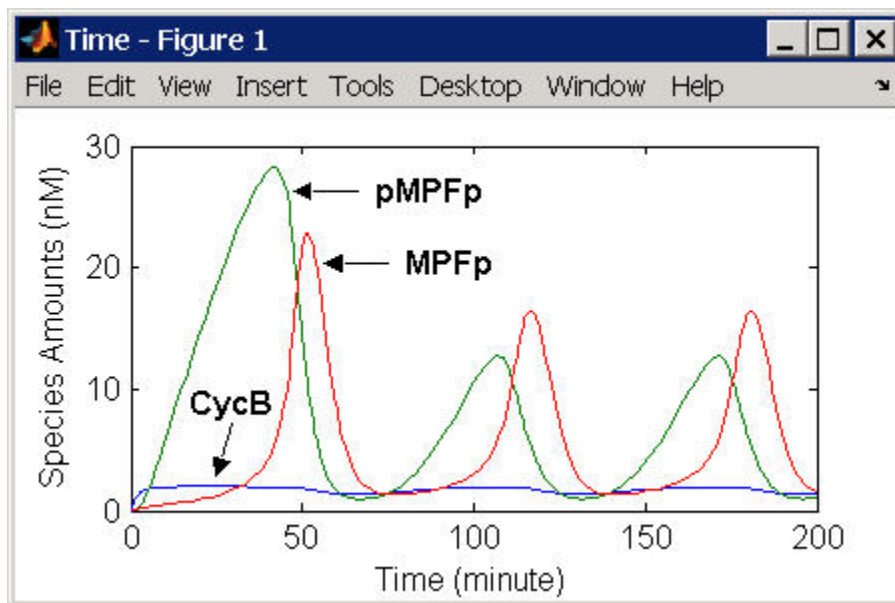
## Algebraic Rule 19, Rate Parameter Kwee1

Kwee1 is a variable rate parameter whose value is determined by the amount of active and inactive Wee1. The algebraic rule is from “Equation 19, Rate Parameter Kwee1” on page 3-12.

```
algebraic rule: Vweei*Wee1p + Vweea*(TotalWee1 - Wee1p) - Kwee1
```

## Simulation of the M-Phase Control Model with Rules

This is a simulation of the M-phase control model using rate and algebraic rules. Simulate with the `sundials` solver and plot species `CycB`, `pMPFp`, and `MPFp`. For a description of the model, see “SimBiology Model with Rate and Algebraic Rules” on page 3-13.



If you want to run the simulation, you can open the model within the SimBiology desktop.

- 1 Open the SimBiology desktop using the function `simbiology`.
- 2 From the **File** menu, select **Open Project**.
- 3 Browse to the file `m_phase_xenopus.sbproj` in the following directory:

`matlabroot/toolbox/simbio/simbiodemom/m_phase_xenopus.sbproj`

For a model using reactions and algebraic rules, see “SimBiology Model with Reactions and Algebraic Rules” on page 3-21.



## SimBiology Model with Reactions and Algebraic Rules

### In this section...

“Overview” on page 3-22

“Reaction 1, Synthesis of Cyclin B ” on page 3-22

“Reaction 2, Degradation of Cyclin B ” on page 3-23

“Reaction 3, Dimerization of Cyclin B with Cdc2 Kinase” on page 3-24

“Reaction 4, Degradation of Cyclin B on MPF” on page 3-25

“Reaction 5, Deactivation of Active MPF” on page 3-26

“Reaction 6, Activation of MPF” on page 3-27

“Reaction 7, Remove Inhibiting Phosphate from Inhibited MPF” on page 3-28

“Reaction 8, Inhibition of MPF by Phosphorylation” on page 3-29

“Reaction 11, Degradation of Cyclin B on Inhibited MPF” on page 3-31

“Reaction 12, Deactivation of MPF to Inhibited MPF” on page 3-31

“Reaction 13, Activation of Inhibited MPF” on page 3-31

“Reaction 15, Degradation of Cyclin B on Active but Inhibited MPF” on page 3-32

“Reaction 16, Inhibit MPF by Phosphorylation” on page 3-32

“Reaction 17, Remove Inhibiting Phosphate from Activated MPF” on page 3-33

“Reaction 19, Degradation of Cyclin B on Activated MPF” on page 3-33

“Reaction 36, Activation of Cdc25 by Activated MPF” on page 3-33

“Reaction 37, Deactivation of Cdc25” on page 3-34

“Reaction 38, Deactivation of Wee1 by Active MPF” on page 3-34

“Reaction 39, Activation of Wee1” on page 3-34

“Reaction 40, Activation of Intermediate Enzyme by Active MPF ” on page 3-35

“Reaction 41, Deactivation of IE” on page 3-35

**In this section...**

“Reaction 42, APC Activation by IEp” on page 3-35

“Reaction 43, APC Deactivation” on page 3-35

“Block Diagram of the M-Phase Control Model with Reactions” on page 3-36

“Simulation of the M-Phase Control Model with Reactions” on page 3-38

## Overview

There can be one or more reactions for an equation defining a species and one algebraic rule for each variable parameter in the M-phase control model [Marlovits 1998]. For a list and description of the equations, see “M-Phase Control Equations” on page 3-4.

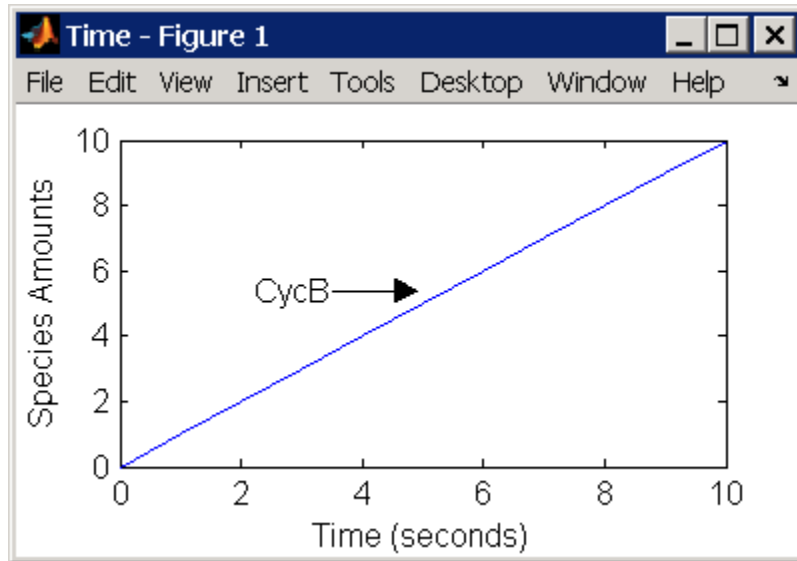
A basic model includes reactions 1 to 8, 11 to 13, 15 to 17, 19, and 36 to 43 with algebraic rules from equations 17, 18, and 19.

## Reaction 1, Synthesis of Cyclin B

Cyclin B is synthesized at a constant rate.

```
reaction: AA -> CycB
reaction rate: k1 nM/minute
parameter: k1 = 1 nM/minute
species: CycB = 0 nM
          AA = 100 nM [x]constant [x]boundary
```

Simulate reaction 1 with the sundials solver.



## Reaction 2, Degradation of Cyclin B

Cyclin B is degraded at the end of the M-phase.

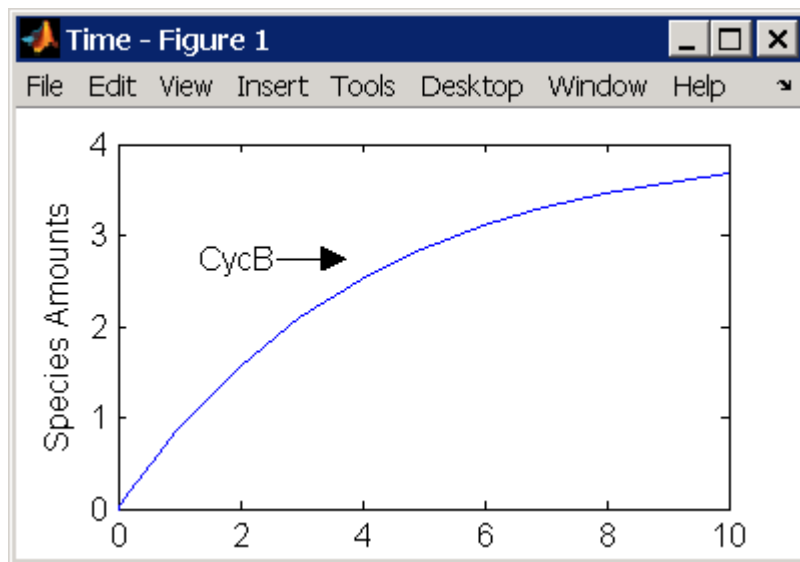
```

reaction: CycB -> AA
reaction rate: K2*CycB nM/minute
parameters: K2 = 0 1/minute, []constant, variable by rule
            V2i = 0.005 1/nM*minute
            V2a = 0.25 1/nM*minute
species: CycB = 0 nM
         APCi = 1 nM
         APCa = 0 nM
         AA = 100 nM [x]constant [x]boundary
algebraic rule: (V2i*APCi) + (V2a*APCa) - K2

```

Initially, Cyclin B degradation is low. This implies the amount of active APC (APCa) = 0 and inactive APC (APCi) = APCtotal = 1 nM.

Test the algebraic rule by simulating reactions 1 and 2 with APCi = 0 and APCa = 1.

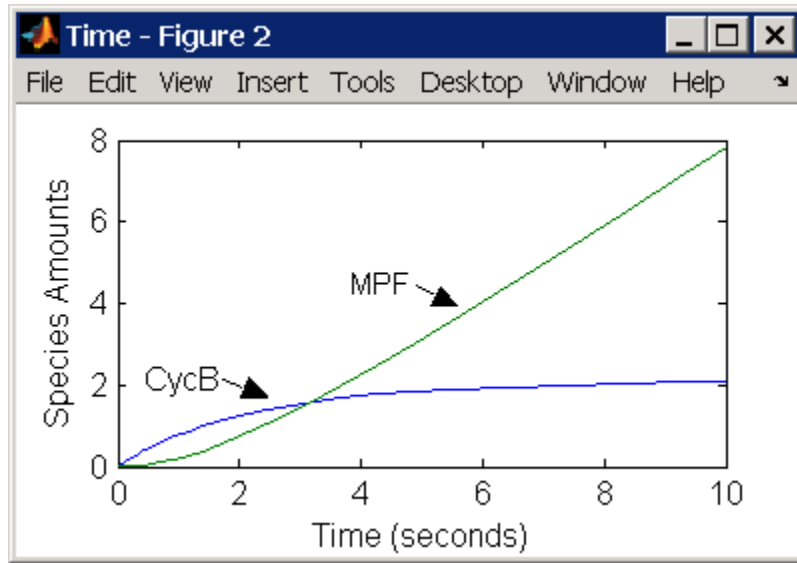


### Reaction 3, Dimerization of Cyclin B with Cdc2 Kinase

Cyclin B dimerizes with Cdc2 kinase to form M-phase promoting factor (MPF).

```
reaction: Cdc2 + CycB -> MPF
reaction rate: k3*Cdc2*CycB nM/minute
parameters: k3 = 0.005 1/(nM*minute)
species: Cdc2 = 100 nM
          CycB = 0 nM
          MPF = 0 nM
```

Test the model by simulating with  $K2 = 0.25$ .



### Reaction 4, Degradation of Cyclin B on MPF

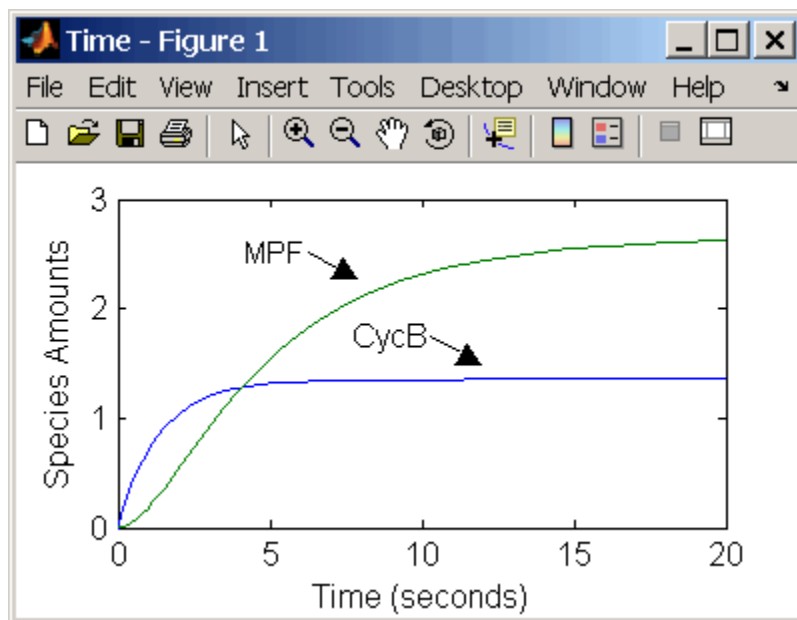
Cyclin B is tagged with ubiquitin groups and degrades while bound to Cdc2.

```

reaction: MPF -> Cdc2 + AA
reaction rate: K2*[MPF]
parameters: K2 = 0 or 0.25 1/minute, variable by rule
             v2i = 0.005 1/(nM*minute)
             v2a = 0.25 1/(nM*minute)
species: MPF = 0 nM
          APCi = 1 nM
          APCa = 0 nM
          AA = 100 nM [x]constant [x]boundary
algebraic rule: (v2i*APCi) + (v2a*APCa) - K2

```

Test the simulation with  $APCa = 1$  and  $APCi = 0$ . Because the amount of  $APCa$  (active) is high,  $K2$  increases and the degradation starts to balance the synthesis of MPF.



### Reaction 5, Deactivation of Active MPF

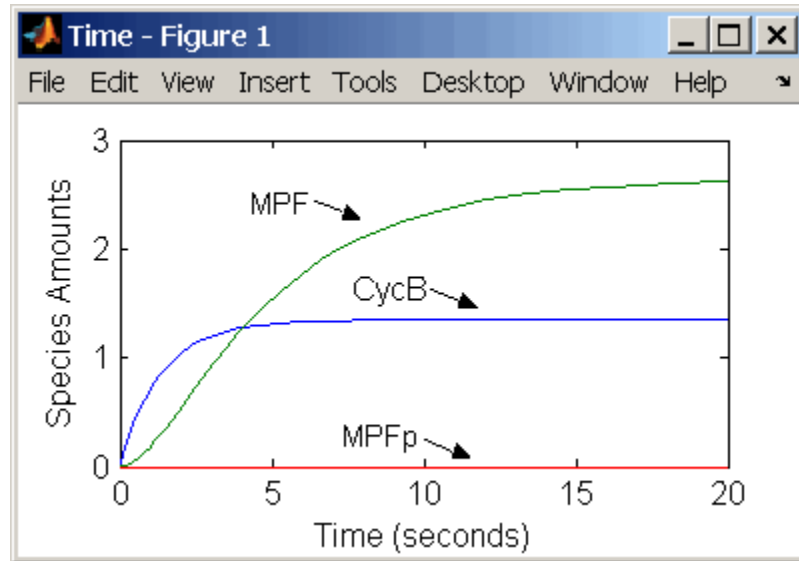
Active MPF (MPFp) is dephosphorylated on Thr-161 by an unknown phosphatase (PP) to inactive MPF (MPF).

```

reaction: MPFp -> MPF
reaction rate: kpp*[MPFp]
parameters: kpp = 0.004 1/minute
species: MPFp = 0 nM
          MPF = 0 nM
    
```

$k_{\text{cacr}} = 0.004$  1/minute [Marlovits 1998, p. 175], but is renamed to  $k_{\text{pp}}$  [Borisuk 1998].

Test simulation with  $\text{APCa} = 1$  and  $\text{APCi} = 0$ . MPF increases without reaching steady state.



### Reaction 6, Activation of MPF

Inactive MPF (MPF) is phosphorylated on Thr-161 by an unknown cyclin activating kinase (CAK).

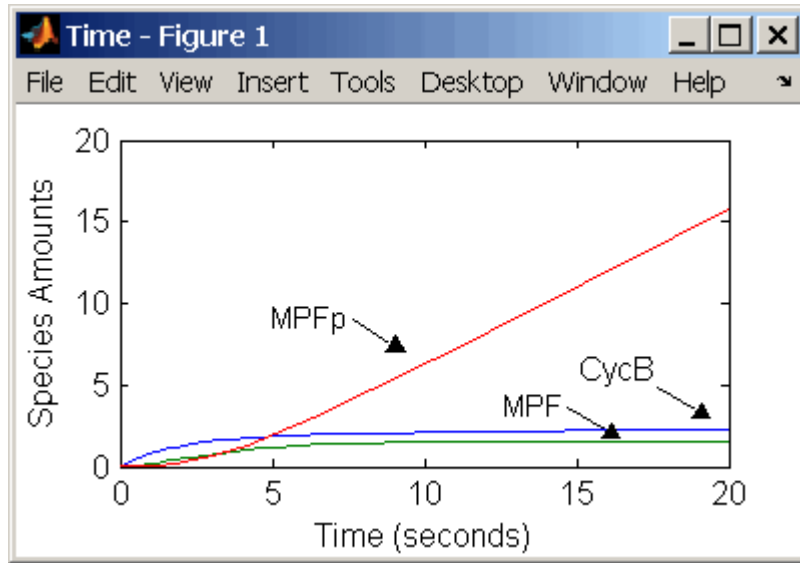
```

reaction: MPF -> MPFp
reaction rate: kcak*[MPF]
parameters: kcak = 0.64 1/minute
species: MPF = 0 nM
          MPFp = 0 nM

```

The kinase reaction that phosphorylates MPF to the active form is 160 times faster than the phosphatase reaction that dephosphorylates active MPF.

Simulate the model with reactions 1 to 6. Notice that after adding reaction 6, most of the product goes to active MPF (MPFp).



### Reaction 7, Remove Inhibiting Phosphate from Inhibited MPF

Cdc25 phosphatase removes the inhibiting phosphate groups at the threonine 14 and tyrosine 15 residues on Cdc2 kinase.

```

reaction: pMPF -> MPF
reaction rate: Kcdc25*[pMPF]
parameters: Kcdc25 = 0.0 1/minute or 0.017 1/minute, variable by
                                                    algebraic rule
                                                    V25i = 0.017 1/(mM*minute)
                                                    V25a = 0.17 1/mM*minute
species: pMPF = 0 nM
        MPF = 0 nM
        Cdc25 = 1 nM (inactive)
        Cdc25p = 0 nM (active)
algebraic rule: (V25i*Cdc25) + (V25a*Cdc25p) - Kcdc25
    
```

Initially, all of the Cdc25 phosphatase is in the inactive form (Cdc25).



Enter the initial value for Kcdc25 as 0.0 and let the first time step calculate the value from the rule, or enter an initial value using the rule.

Initially, set **ConstantAmount** for Cdc25 and Cdc25p to test reactions 1 through 7. Then after you can add the reactions to regulate the Cdc25 phosphatase by clearing the **ConstantAmount** property.

## Reaction 8, Inhibition of MPF by Phosphorylation

Addition of inhibiting phosphate groups by Wee1 kinase to inhibit active M-phase promoting factor (MPF). Myt1 kinase is also involved with the phosphorylation, but its contribution is grouped with Wee1.

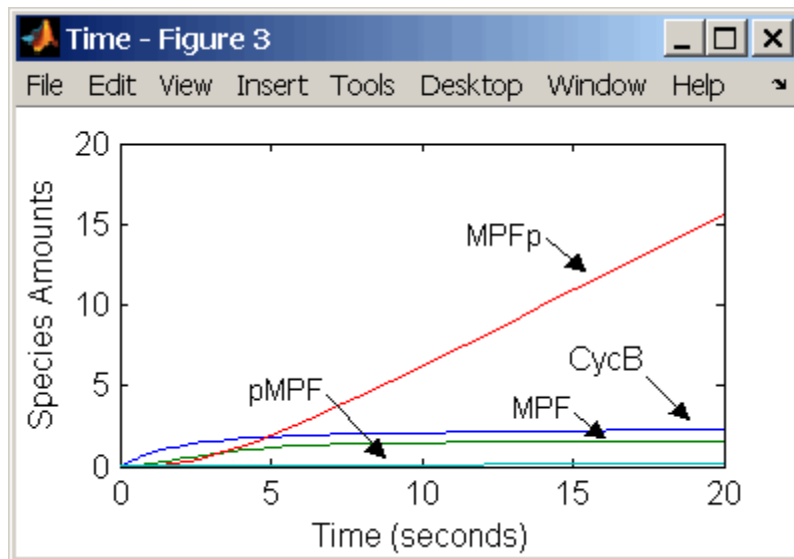
```

reaction: MPF -> pMPF
reaction rate: Kwee1*[MPF]
parameters: Kwee1 = 0.0 1/minute or 0.01 1/minute, variable by
                                                    algebraic rule
            Vwee1i = 0.01 1/(nM*minute)
            Vwee1a = 1.0 1/(nM*minute)
species: MPF = 0 nM
        pMPF = 0 nM
        Wee1p = 1 nM (inactive)
        Wee1 = 0 nM (active)
algebraic rule: (Vwee1i*Wee1p) + (Vwee1a*Wee1) - Kwee1

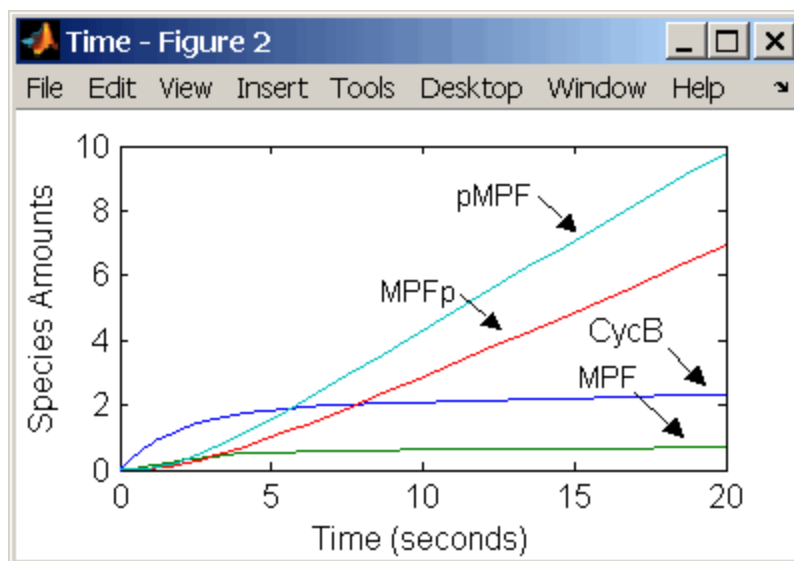
```

The initial capitalization for the parameter Kwee1 is a convention to indicate that this value changes during the simulation.

Test the simulation for reactions 1 through 8 with Wee1p (inactive) = 1 and Wee1 (active) = 0.



Test the simulation with Wee1p (inactive) = 0 and Wee1 (active) = 1.



## Reaction 11, Degradation of Cyclin B on Inhibited MPF

Degradation of cyclin B (CycB) on inhibited MPF (pMPF). Cyclin B is tagged with ubiquitin groups and degrades while bound to Cdc2.

```

reaction: pMPF -> Cdc2 + AA
reaction rate: K2*[pMPF] nM/minute
parameters: K2 = 0 or 0.25 1/minute, variable by rule
            V2i = 0.005 1/nM*minute
            V2a = 0.25 1/nM*minute
species: MPF = 0 nM
        APCi = 1 nM
        APCa = 0 nM
        AA = 100 nM [x]constant [x]boundary
        Cdc2 = 100 nm
algebraic rule: (V2i*APCi) + (V2a*APCa) - K2

```

Test the simulation with Wee1 active (Wee1 = 1) and APC active (APCi = 1).

## Reaction 12, Deactivation of MPF to Inhibited MPF

Inhibited/active MPF (pMPFp) is dephosphorylated on Thr-161 by an unknown phosphatase (PP) to inhibited MPF (pMPF). Compare reaction 12 with reaction 5.

```

reaction: pMPFp -> pMPF
reaction rate: kpp*[pMPFp]
parameters: kpp = 0.004 1/minute
species: pMPFp = 0 nM
        pMPF = 0 nM

```

## Reaction 13, Activation of Inhibited MPF

Inhibited MPF (pMPF) is phosphorylated on Thr-161 by an unknown cyclin-activating kinase (CAK). Compare reaction 13 with reaction 6.

```

reaction: pMPF -> pMPFp
reaction rate: kca*[pMPF] nM/minute
parameters: kca = 0.64 1/minute
species: pMPF = 0 nM

```

pMPFp = 0 nM

Test the simulation with Wee1p = 1 (inactive)/ Wee1 = 0 and then test with Wee1p = 0 (inactive)/ Wee1 = 1.

### Reaction 15, Degradation of Cyclin B on Active but Inhibited MPF

Degradation of cyclin B (CycB) on inhibited MPF (pMPF). Cyclin B is tagged with ubiquitin groups and degrades while bound to cdc2 kinase.

```

reaction: pMPFp -> Cdc2 + AA
reaction rate: K2*[pMPFp] nM/minute
parameters: K2 = 0 or 0.25 1/minute, variable by rule
             v2i = 0.005 1/nM*minute
             v2a = 0.25 1/nM*minute
species: MPF = 0 nM
          APCi = 1 nM
          APCa = 0 nM
          AA = 100 nM [x]constant [x]boundary
          Cdc2 = 100 nm
algebraic rule: (V2i*APCi) + (V2a*APCa) - K2
    
```

### Reaction 16, Inhibit MPF by Phosphorylation

Addition of inhibiting phosphate groups by Wee1 kinase to inhibit active M-phase promoting factor (MPF). Myt1 kinase is also involved with the phosphorylation, but its contribution is grouped with Wee1.

```

reaction: MPFp -> pMPFp
reaction rate: Kwee1*[MPFp] nM/minute
parameters: Kwee1 = 1/minute [x]constant, variable by rule
             Vweei = 0.01 1/nM*minute
             Vweea = 1 1/nM*minute
species: MPFp = 0 nM
          pMPFp = 0 nM
          Wee1p = 1 nM (inactive)
          Wee1 = 0 nM (active)
algebraic rule: (Vwee1i*Wee1p) + (Vwee1a*Wee1) - Kwee1
    
```

## Reaction 17, Remove Inhibiting Phosphate from Activated MPF

Remove the inhibiting phosphate group from pMPFp with cdc25 phosphatase.

```

reaction: pMPFp -> MPFp
reaction rate: Kcdc25*[pMPFp]
parameters: Kcdc25 = 0 1/minute, [x]constant, variable by rule
            V25i = 0.017 1/nM*minute
            V25a = 0.17 1/nM*minute
species: pMPFp = 0 nM
        MPFp = 0 nM
algebraic rule: (V25i*Cdc25) + (V25a*Cdc25p) - Kcdc25

```

## Reaction 19, Degradation of Cyclin B on Activated MPF

Degradation of cyclin B (CycB) on inhibited MPF (pMPF). Cyclin B is tagged with ubiquitin groups and degrades while bound to cdc2 kinase.

```

reaction: MPFp -> MPF + AA
reaction rate: K2*[MPFp] nM/minute
parameters: K2 = 0 or 0.25 1/minute, variable by rule
            V2i = 0.005 1/nM*minute
            V2a = 0.25 1/nM*minute
species: MPF = 0 nM
        MPFp = 0 nM
        APCi = 1 nM
        APCa = 0 nM
        AA = 100 nM [x]constant [x]boundary
        Cdc2 = 100 nm
algebraic rule: (V2i*APCi) + (V2a*APCa) - K2

```

## Reaction 36, Activation of Cdc25 by Activated MPF

Activation of cdc25 phosphatase by phosphorylation with active M-phase promoting factor (MPFp).

```

reaction: Cdc25 + (MPFp) -> Cdc25p + (MPFp)
reaction rate: (k25*[MPFp]*[Cdc25])/(Km25 + [Cdc25])
parameters: k25 = 0.02 1/minute

```

Km25 = 0.1 nM  
species: Cdc25 = 1 nM (inactive)  
Cdc25p = 0 nM (active)

Initially MPF is inhibited (MPF\* reacts to pMPF\*).

### Reaction 37, Deactivation of Cdc25

Deactivation of cdc25 phosphatase by dephosphorylation with an unknown phosphatase.

reaction: Cdc25p -> Cdc25  
reaction rate:  $(k_{25r} * [Cdc25p]) / (K_{m25r} + [Cdc25p])$   
parameters: k25r = 0.1 nM/minute  
Km25r = 1 nM  
species: Cdc25 = 1 nM (inactive)  
Cdc25p = 0 nM (active)

### Reaction 38, Deactivation of Wee1 by Active MPF

Deactivation of Wee1 kinase by phosphorylation with active M-phase promoting factor (MPFp).

reaction: Wee1 + (MPFp) -> Wee1p + (MPFp)  
reaction rate:  $(k_w * [MPFp] * [Wee1]) / (K_{mw} + [Wee1])$  nM/minute  
parameters: kw = 0.02 1/minute  
Kmw = 0.1 nM  
species: Wee1p = 1 nM (inactive)  
Wee1 = 0 nM (active)

Initially MPF is inhibited (MPF\* reacts to pMPF\*).

### Reaction 39, Activation of Wee1

Activation of Wee1 kinase by dephosphorylation with an unknown kinase.

reaction: Wee1p -> Wee1  
reaction rate:  $(k_{wr} * [Wee1p]) / (K_{mwr} + [Wee1p])$  nM/minute  
parameters: kwr = 0.1 nM/minute  
Kmwr = 1 nM  
species: Wee1p = 1 nM (inactive)

Wee1 = 0 nM (active)

### Reaction 40, Activation of Intermediate Enzyme by Active MPF

The inactive intermediate enzyme (IE) is activated by phosphorylation with active M-phase promoting factor (MPFp).

```

reaction: IE + (MPFp) -> IEp + (MPFp)
reaction rate: (kie*[MPFp]*[IE])/(Kmie + [IE])
parameters: kie = 0.02 1/minute
             Kmie = 0.01nM
species: IE = 1 nM (inactive)
         IEp = 0 nM (active)

```

### Reaction 41, Deactivation of IE

The active intermediate enzyme (IE) is deactivated by dephosphorylation.

```

reaction: IEp -> IE
reaction rate: (kier*[IEp])/(Kmier + [IEp])
parameters: kier = 0.15 nM/minute
             Kmier = 0.01 nM
species: IE = 1 nM (inactive)
         IEp = 0 nM (active)

```

### Reaction 42, APC Activation by IEp

Anaphase-promoting complex (APC) is activated by an active intermediate enzyme (IEp).

```

reaction: APCi + IEp -> APCa + IEp
reaction rate: (kap*[IEp]*[APCi])/(Kmap + [APCi])
parameters: kap = 0.13 1/minute
             Kmap = 0.01 nM
species : APCi = 1 nM
         APCa = 0 nM

```

### Reaction 43, APC Deactivation

Anaphase-promoting complex (APC) is deactivated.

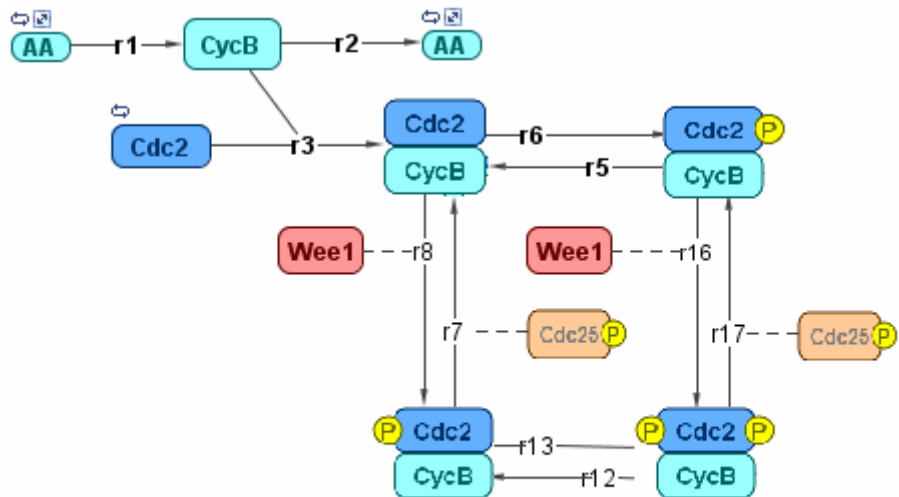
```

reaction: APCa -> APCi

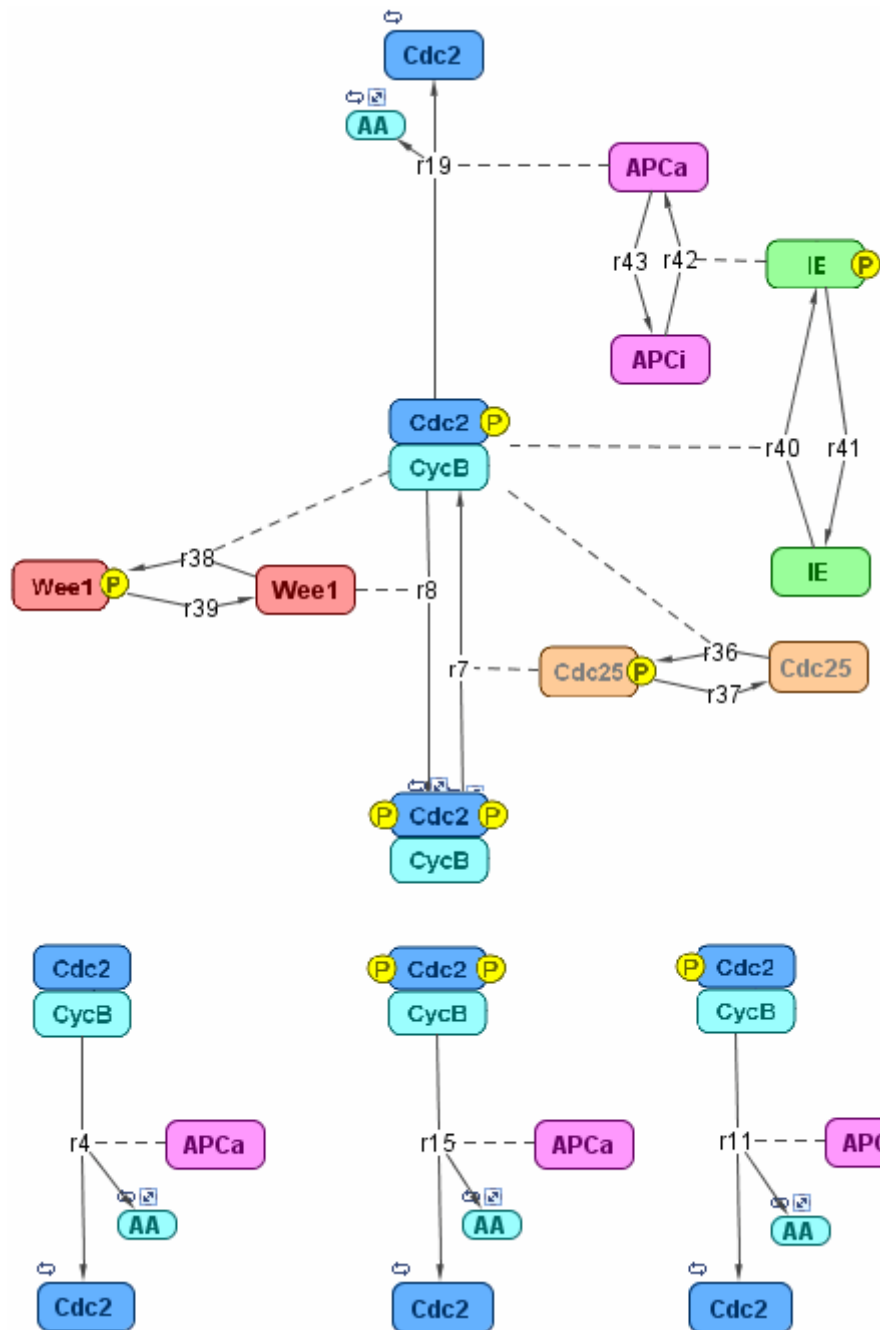
```

reaction rate:  $(k_{apr} * [APCa]) / (K_{mapr} + [APCa])$   
 parameters:  $k_{apr} = 0.13$  nM/minute  
 $K_{mapr} = 1$  nM  
 species :  $APCi = 1$  nM  
 $APCa = 0$  nM

### Block Diagram of the M-Phase Control Model with Reactions

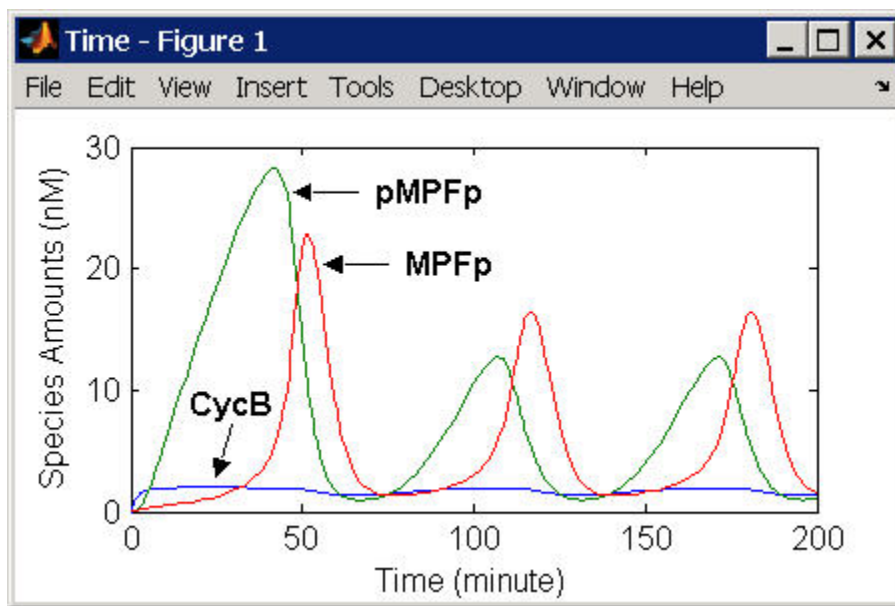






## Simulation of the M-Phase Control Model with Reactions

This is a simulation of the M-phase control model using reactions and algebraic rules. Simulate with the `sundials` solver and plot species `CycB`, `pMPFp`, and `MPFp`. For a description of the model, see “SimBiology Model with Reactions and Algebraic Rules” on page 3-21.



If you want to run the simulation, you can open the model within the SimBiology desktop.

- 1 Open the desktop using the function `simbiology`.
- 2 From the **File** menu, select **Open Project**.
- 3 Browse to the file `m_phase_xenopus.sbproj` in the following directory:

```
matlabroot/toolbox/simbio/simbiodemodemos/m_phase_xenopus.sbproj
```

For a model using reactions and algebraic rules, see “SimBiology Model with Reactions and Algebraic Rules” on page 3-21.

## References

- [1] Borisuk M, Tyson J (1998), “Bifurcation analysis of a model of mitotic control in frog eggs,” *Journal of Theoretical Biology*, 195(1):69–85, PubMed 9802951.
- [2] Marlovits G, Tyson C, Novak B, Tyson J (1998), “Modeling M-phase control in *Xenopus* oocyte extracts: the surveillance mechanism for unreplicated DNA,” *Biophysical Chemistry*, 72(1-2):169–184, PubMed 9652093.
- [3] Novák B, Tyson J (1993), “Numerical analysis of a comprehensive model of M-phase control in *Xenopus* oocyte extracts and intact embryos,” *Journal of Cell Science*, 106(4):1153–1168, PubMed 8126097.



## G

- G protein cycle
  - background 2-3
  - in yeast 2-3
  - model 2-1
  - modeling of 2-5
- G protein cycle model
  - experimental data and assumptions 2-5
  - reactions overview 2-5
- G proteins
  - introduction 2-3

## M

- models
  - G protein cycle 2-1

## R

- references
  - yeast G protein cycle model 2-52

## Y

- yeast G protein cycle model
  - add reaction 2-13
  - change simulation settings of 2-27
  - comparison of

- active G protein fractions 2-44
- copy and change 2-34
- creating a rule 2-25
- custom plot 2-37
  - data from two models 2-45
- determine rate equation 2-15
- experimental and simulation data
  - comparison of 2-48
  - custom plot 2-48
- experimental data and assumptions 2-5
- graphical representation 2-5
- in SimBiology 2-10
- introduction 2-1 2-5
- mutant strain 2-37
- open SimBiology desktop 2-11
- parameters table 2-22
- project file 2-12
- reactions overview 2-5
- reactions table 2-19
- references 2-52
- setting species initial amounts 2-18
- simulation results
  - sst2Δ* 2-35
  - wild-type 2-31
- species table 2-23
- tutorial goals 2-10
- wild-type strain 2-10